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Inter-Scale Similarity Guided Cost Aggregation for Stereo Matching

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Ahene,—Serve matching sina to estimate 3D geometry by The well-known prigeine divides steres matching

is computed descripti *Abstract*— Stereo matching aims to estimate 3D geometry by computing disparity from a rectified image pair. Most deep learning based stereo matching methods aggregate multi-scale cost volumes computed by downsampling and achieve good performance. However, their effectiveness in fine-grained areas is limited by significant detail loss during downsampling and the use of fixed weights in upsampling. In this paper, we propose an inter-scale similarity-guided cost aggregation method that dynamically upsamples the cost volumes according to the content of images for stereo matching. The method consists of two modules: inter-scale similarity measurement and stereo-content- aware cost aggregation. Specifically, we use inter-scale similarity measurement to generate similarity guidance from feature maps in adjacent scales. The guidance, generated from both reference and target images, is then used to aggregate the cost volumes from low-resolution to high-resolution via stereo-content-aware cost aggregation. We further split the 3D aggregation into 1D disparity and 2D spatial aggregation to reduce the computational cost. Experimental results on various benchmarks (e.g., Scene- Flow, KITTI, Middlebury and ETH3D-two-view) show that our method achieves consistent performance gain on multiple models (e.g., PSM-Net, HSM-Net, CF-Net, FastAcv, and FactAcvPlus). The code can be found at https://github.com/Pengxiang-Li/issga-²⁴ stereo.

²⁵ *Index Terms*— Stereo matching, cost aggregation, content-²⁶ aware upsampling.

27 **I. INTRODUCTION**

28 STEREO matching aims to estimate a pixel-wise dis-
29 parity map from a rectified image pair. It plays an
important role in verious emplications including 2D room. ³⁰ important role in various applications including 3D recon- $_{31}$ struction [1], AR [2], SLAM [3], and autonomous driving [4].

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The well-known pipeline divides stereo matching into four 32 steps: cost computation, cost aggregation, disparity computa-
33 tion, and disparity refinement $[5]$. Among these four steps, $\frac{34}{4}$ cost aggregation plays a pivotal role in leveraging neighbor- ³⁵ hood information to rectify the ambiguous matching costs in 36 ill-posed regions such as occluded regions, large textureless 37 areas, repetitive patterns, and thin structures. The cost aggre- ³⁸ gation is commonly embedded into end-to-end deep neural 39 networks with multi-scale processing to enlarge the receptive 40 field. 3D CNNs $[6]$, $[7]$, GRU $[8]$, $[9]$, and attention mecha- 41 nism $[10]$ are the most commonly used basic structures for cost 42 aggregation, effectively correcting ambiguous matching costs 43 and substantially enhancing prediction accuracy in ill-posed 44 regions by aggregating multi-scale cost volumes. ⁴⁵

However, these cost aggregation methods often struggle in 46 fine-grained areas due to considerable detail loss during down- ⁴⁷ sampling and fixed weight used in upsampling. Many efforts 48 have been targeted at improving the performance of stereo 49 matching in fine-grained areas, including edge information 50 [11], deformable convolutions $[12]$, group-wise correlation 51 [13] and slanted planes [14]. These methods have achieved 52 good performance, but two challenging problems in cost 53 aggregation are still not well solved: (1) the downsampling 54 causes considerable detail loss during the construction of ⁵⁵ multi-scale cost volumes, and (2) the upsampling fixed in size $\frac{56}{60}$ and weight is prone to data imbalance between large-smooth 57 areas and fine-grained areas. For example, the HSM-Net [7] 58 with multi-scale cost volumes and upsampling fixed in size and 59 weight may lead to poor performance in fine-grained areas, $\overline{60}$ as illustrated in Fig. 1 (b) and Fig. 1 (c). $\qquad \qquad \text{61}$

In this paper, we propose inter-scale similarity-guided cost 62 aggregation that adaptively restores image details by dynam- 63 ically upsampling cost volumes based on image content. ⁶⁴ Our method comprises two modules: inter-scale similar- ⁶⁵ ity measurement and stereo-content-aware cost aggregation. 66 We utilize inter-scale similarity measurements to generate 67 similarity guidance from the feature maps of adjacent scales. 68 Subsequently, we employ this guidance to aggregate the 69 multi-scale cost volumes through stereo-content-aware cost 70 aggregation.

For the first challenging problem, our idea is to retrieve $\frac{72}{2}$ the fine-grained details lost during the downsampling pro- ⁷³ cess. We use inter-scale similarity measurement to measure $\frac{74}{6}$ the similarity between high-resolution and low-resolution 75 features. The similarity explicitly preserves the connection ⁷⁶ between high-resolution details and low-resolution features, 77

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Fig. 1. Predictions and upsampling weights visualizations of HSM-Net [7] using different upsampling strategies.

 thereby providing guidance for the upsampling process to restore details. Technically, we first project a point *xhigh* from high-resolution to low-resolution features *xlo*w. Then 81 we compute the similarity between the point in the high- α resolution x_{high} and the neighbors of the projected point in low-resolution N*lo*w.

 For the second challenging problem, a critical factor leading to the suboptimal restoration of fine-grained details is the fixed size and weights of existing upsampling strategies, 87 which are unable to adapt to the complicated fine-grained details. Motivated by this, we replace the fixed upsampling with content-aware upsampling. The content-aware upsam- pling uses the content information of each point to guide the upsampling process, thereby mitigating the impact of data imbalance between large-smooth and fine-grained areas. 93 In stereo-content-aware cost aggregation, we use similarity guidance (generated from both reference and target images) to guide the aggregation of matching costs in 3D spatial-disparity space. The pair-wise 3D upsampling is computationally expen- sive. Thus, we split the upsampling in the 3D space into 1D disparity and 2D spatial space. As a result, our method is able to efficiently and adaptively assemble the proper neighbors for cost aggregation and upsampling. Our method generates upsampling weight according to the image content and achieves much finer details, as shown in Fig. 1 (d). Our method can be plugged into any multi-scale cost volume based stereo network and achieve higher accuracy, especially in fine-grained areas.

¹⁰⁶ Our contributions are summarized as follows:

¹⁰⁷ 1) We propose an inter-scale similarity guided cost aggre-¹⁰⁸ gation method to adaptively recover the details of cost volumes under the guidance of similarity generated from 109 images. 110

- 2) We introduce an inter-scale similarity measurement to 111 dynamically generate guidance by incorporating infor- ¹¹² mation from both low-resolution and high-resolution 113 feature maps. The explicit utilization of high-resolution 114 feature maps ensures the preservation of fine-grained 115 details. 116
- 3) We design a decomposition strategy that splits 3D 117 disparity-spatial upsampling into 1D disparity and 2D 118 spatial upsampling, significantly reducing the computa-
119 tional cost of the 3D pair-wise upsampling.

II. RELATED WORK 121

A. Stereo Matching 122

Traditional stereo matching methods estimate disparity ¹²³ maps for rectified image pairs using local [15], [16], 124 global [17], [18], and semi-global methods [19], [20], [21]. ¹²⁵ Deep learning-based stereo matching networks now dominate, 126 delivering state-of-the-art results. Early deep learning methods 127 replaced steps in stereo matching $[5]$: cost computation $[22]$, 128 [23], [24], cost aggregation [25], [26], [27], disparity compu-
129 tation $[28]$, and disparity refinement $[26]$, $[27]$. Despite good 130 performance, their non-end-to-end approaches limited data 131 utilization. To overcome this, end-to-end methods compute 132 correlations by warping the target image to the reference 133 image $[8]$, $[9]$, $[11]$, $[29]$. These achieve excellent results but 134 often lose geometric information. Cost-volume-based mod- ¹³⁵ els [6], [30], [31], [32], [33], [34], [35] preserve geometric ¹³⁶ information by concatenating multi-scale cost volumes. State- ¹³⁷ of-the-art methods use convolution neural networks [36], [37], ¹³⁸ [38], [39], [40], [41] or attention mechanisms [10], [42], [43], 139 [44] to aggregate these volumes, effectively utilizing image 140 context information. 141

However, multi-scale cost volume-based stereo matching 142 methods often lose fine-grained details due to downsampling. 143 While cost aggregation usually recovers these details, current 144 fixed-size and fixed-weight schemes struggle with data imbal- ¹⁴⁵ ances between large smooth, and fine-grained areas. To address 146 this, we developed a content-aware cost aggregation method ¹⁴⁷ that mitigates detail loss during multi-scale cost volume cre- ¹⁴⁸ ation. Our adaptive upsampling approach also remains robust ¹⁴⁹ against data imbalances. 150

B. Cost Aggregation 151

Multi-scale cost aggregation methods [6], [29] enhance 152 matching cost reliability by optimizing multi-scale cost volumes for precise disparity estimation. Song et al. [11] used 154 edge information to guide cost aggregation, reducing edge mis- ¹⁵⁵ matches. Zhang et al. $[45]$ improved efficiency by replacing 3D $_{156}$ CNNs with semi-global aggregation. Yang et al. [7] proposed a 157 hierarchical feature volume decoder for high-resolution image 158 disparity estimation. Xu et al. $[12]$ utilized deformable convolution for adaptive aggregation. Lipson et al. $[8]$ designed 160 an iterative mixed disparity sampling and aggregation strategy. ¹⁶¹ Liu et al. [46] used local features to address over-smoothing. 162 Zhang et al. [47] introduced depth-based sampling for bal- anced density in close and far regions. Xu et al. [48] utilized ¹⁶⁵ bilateral grid processing for faster aggregation. Lee et al. [49] introduced a cluster-wise cost aggregation algorithm to paral-lelized scanline-level disparity computation.

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manual variable can be formulated. The generation of the control of the
state in the state of the state of the state of the state of the state of
the state of the state of the state in the s The aforementioned methods demonstrate commendable performance, even in ill-posed areas. However, they still suffer from the loss of details in downsampling, and their strategies for multi-scale cost aggregation are susceptible to data imbalance. These strategies commonly rely on either bilinear interpolation or deconvolution for upsampling. Both bilinear interpolation and deconvolution employ a fixed inter- polation rule or deconvolution kernel across all data points, thus failing to exploit the content information of images fully. Constrained by computational memory limitations, these methods are unable to perform direct aggregation at full resolution. Instead, they resort to upsampling to full resolution without introducing additional parameters after aggregat- ing at 1/2 or 1/4 resolution. However, relying solely on parameter-free upsampling is inadequate for recovering lost ¹⁸³ details.

¹⁸⁴ *C. Upsampling*

 Upsampling is used to transform data from low-resolution to high-resolution. Traditional upsampling strategies fit a curve of a small neighborhood of the upsampled points to com- pute values for interpolated points, including nearest neighbor interpolation [50], bilinear interpolation [51], trilinear interpo- lation [52], and bicubic interpolation [53], etc. The advantage of these methods lies in their low computational cost. How- ever, these parameter-free upsampling strategies underutilize image content, resulting in blurred recovery results in fine- grained areas. Deconvolution [54], [55], [56], [57] offers a learning-based approach to upsampling, where weights are optimized through backpropagation. Learning-based upsam- pling kernels enable the utilization of contextual information learned from extensive data. However, deconvolution has lim- itations as it struggles in various scenes due to fixed kernel sizes and weights, making it susceptible to data imbalances.

201 Several works $[58]$, $[59]$, $[60]$ use content-aware upsampling operators to solve the fixed-weight problem. Wang et al. $[58]$, [59] presented a content-aware reassembly approach and argued that traditional feature upsampling methods struggle to capture rich semantic information. While content-aware upsampling mitigates the fixed-weight problem, it relies solely on information from the low-resolution side (i.e., the upsam- pling process could be regarded as a unary low-resolution to high-resolution mapping). However, the upsampling process inherently consists of both low-resolution and high-resolution components, and relying solely on low-resolution features for upsampling may not suffice. Instead of employing a unary upsampling mapping, we introduce an inter-scale similarity measurement approach to produce a pair-wise upsampling mapping, represented by similarity guidance derived from information gathered across adjacent scales. In other words, we actually model the upsampling process as a binary mapping between low-resolution and high-resolution.

III. OPTIMIZATION IN MULTI-SCALE COST AGGREGATION 219

In this section, we model the optimization objectives for 220 each layer of multi-scale cost aggregation. Given a cost volume 221 $C_{l-1} \in \mathbb{R}^{H_{l-1} \times W_{l-1} \times D_{l-1}}$ at level $l-1$ as input, C_l is computed 222 via a network with learning weights W_l . The generation of C_l 223 can be formulated as 224

$$
p(C_l) = p(C_l|C_{l-1}, W_l)p(W_l)p(C_{l-1})
$$

$$
=p(C_l|C_{l-1},W_l)p(W_l). \qquad (1) \quad \text{226}
$$

The probability $p(C_l)$ of cost volume is commonly computed 227 by $p(C_l)$ = softmax($-C_l$), and $p(C_{l-1})$ is supposed to be 1 as 228 C_{l-1} has already been given. Then, the optimization objective 229 is to find the best W_l , that recovers the details lost in C_{l-1} , 230 is to find the best W_l that recovers the details lost in C_{l-1} , which can be formulated as 231

$$
W_l = \underset{W_l}{\text{argmax}} \ p(W_l | C_l, C_{l-1}), \tag{232}
$$

$$
= \underset{W_l}{\text{argmax}} \ p(W_l|C_l), \tag{233}
$$

$$
= \underset{W_l}{\text{argmax}} \ \frac{\text{p}(C_l|W_l) \cdot \text{p}(W_l)}{\sum_{W_l} \text{p}(C_l|W_l)\text{p}(W_l') dW_l'}, \qquad \qquad \text{234}
$$

$$
\stackrel{a.s.}{=} \underset{W_l}{\text{argmax}} \ p(C_l|W_l) \cdot p(W_l), \qquad \qquad \text{235}
$$

$$
\stackrel{a.s.}{=} \operatorname*{argmax}_{W_l} p(C_l). \tag{2}
$$

In the aforementioned cost aggregation process, it becomes 237 impractical to recover the details lost during downsampling 238 using bilinear upsampling or deconvolution. This is because 239 *W*_l is optimized by cost volumes at level $[0, 1, \ldots, l-1]$, and 240 it doesn't consider the image content at level *l*. In other words, ²⁴¹ only minimal details at level l contribute to the optimization of $_{242}$ W_l . Furthermore, the kernel weights are influenced by the content that appears more frequently in the image. Consequently, ²⁴⁴ it becomes challenging to utilize these fixed kernel weights ²⁴⁵ effectively for recovering details that constitute only a small ²⁴⁶ proportion of the image content such as the fine-grained areas. ²⁴⁷

IV. PROPOSED METHOD ²⁴⁸

A. Problem Formulation ²⁴⁹

Detail loss and biased upsampling are two challenging ²⁵⁰ problems that cause poor performance in fine-grained areas. ²⁵¹ To address these two problems, we optimize cost aggregation 252 with image features at levels *l* and *l* − 1. In our method, 253 the optimization objective of cost aggregation at each level 254 is given by ²⁵⁵

$$
W_l = \underset{W_l}{\operatorname{argmax}} \, \mathrm{p}(C_l) \cdot \mathrm{p}(W_l | F_l, F_{l-1}), \tag{3}
$$

where F_l is the feature map at level *l*.

In particular, the optimization objective of cost aggregation 258 with deconvolution is actually one special case of ours, where 259 $p(W_l|F_l, F_{l-1}) = p(W_l)$. Besides, the optimization objective 260 of cost aggregation with bilinear interpolation is one special ²⁶¹ case of deconvolution, i.e., Eq. (2). With substituting $p(W_l) =$ 262 1 into Eq. (2) , Eq. (2) can be reformulated as 263

$$
W_l = \underset{W_l}{\text{argmax}} \ p(C_l), \tag{4}
$$

Fig. 2. The visualization of aggregation weight and disparity distribution in cost volume. The upper row shows the aggregation weight and the under row shows the distribution of the cost volume along the disparity dimension for a single point. The point in each distribution map is the ground truth for the point in the reference image. Both the bilinear upsampling and deconvolution predict wrong results, while ours not only predicts the correct disparity but also corrects for multi-modality in the distribution.

²⁶⁵ which is just the optimization objective of cost aggregation ²⁶⁶ with bilinear interpolation.

Example the control of the control of the control of the set of (h, w) **and the best
since the control of the set of the s** $_{267}$ In our method, W_l is automatically adjusted from the 268 change of F_l and F_{l-1} during inference, whereas the weights of deconvolution or bilinear interpolation remain static. Our method generates aggregation weight related to the image content and achieves unimodal distribution results, while oth- ers get multimodal distribution or wrong distribution. Fig. 2 provides a visual representation of aggregation using various upsampling strategies. As shown in Fig. 2, the weights for bilinear interpolation remain constant, the weights for decon- volution are repetitive kernels, while our method's weights are content-aware, closely linked to the image's content. It's also worth noting that our method effectively addresses the issue of multiple peaks in the disparity distribution (see the distribution curves of Deconvolutions vs. Ours in Fig. 2). In our method, the disparity distribution exhibits only a single prominent peak precisely at the ground truth disparity, whereas deconvolution may exhibit multiple peaks, potentially leading to incorrect disparity results.

²⁸⁵ *B. Implementation*

 Given an image pair, we extract multi-scale feature maps F_l at each level *l* for reference and target images. We then use the feature maps to construct the cost volume at the lowest level. As for the cost volume at the high level, we iteratively upsample the cost volume from the low level to the high level through two steps, the inter-scale similarity measurement, and the stereo-content-aware cost aggregation. The inter-scale similarity measurement uses feature maps from adjacent scales to generate similarity guidance. The stereo-content-aware cost aggregation uses the similarity guidance from two views to guide the cost volume upsampling. At last, we use the cost volume at the highest level to compute the disparity map as the output of our network. Fig. 3 illustrates the pipeline of our ²⁹⁹ method.

³⁰⁰ *1) Inter-Scale Similarity Measurement:* The inter-scale sim-301 ilarity measurement takes the feature maps F_l and F_{l-1} as input. We compute the similarity by the summation of the input. We compute the similarity by the summation of the

products of $F_l(h', w')$ and the neighbors of $F_{l-1}(h, w)$ with 303 the formula as 304

$$
S_l(h', w') = \frac{1}{M \cdot M} \phi\left(\sum_{(h, w) \in \mathcal{N}_F} F_l(h', w') F_{l-1}(h, w)\right), \quad (5) \quad \text{as}
$$

where (h', w') and (h, w) are the location at high-level and 306 low-level respectively, $(h', w') = (h \cdot s, w \cdot s)$, *s* is the scale 307 change in resolution from level $l - 1$ to level l , and \cdot is the 308 scalar multiplication operation. $S_l \in \mathbb{R}^{H^l \times W^l}$ is the similarity ³⁰⁹ guidance at level *l*, $S_l(h', w')$ is the value of the pixel at σ ³¹⁰ location (h', w') , $\mathcal{N}_F \in \mathbb{R}^{M \times M}$ is a 2D neighborhood of the 311 pixel at location (h, w) with the size of $M \times M$. $\phi(\cdot)$ is a ³¹² subnetwork composed of convolution layers, relu layers, and ³¹³ subnetwork composed of convolution layers, relu layers, and batch normalization layers. 314

2) Stereo-Content-Aware Cost Aggregation: 3D convolution 315 based methods [6], [7] usually perform window based cost 316 aggregation: 317

$$
\mathbf{C}_l(h', w', d') = \sum_{(h, w, d) \in \mathcal{N}_c} \mathbf{W}_l(h', w', d') \mathbf{C}_{l-1}(h, w, d), \quad (6)
$$

where \mathcal{N}_c is a 3D neighborhood of the point at \mathfrak{so} (*h*′ /*s*, w′ /*s*, *d*′ $/$ *s*). 320

In our method, we replace the 3D weight W_l with the 321 2D similarity guidance S_l . For each level, we use the feature 322 maps of the stereo images, i.e., reference and target images, 323 to compute the content-aware similarity guidance S_l^R and S_l^T *l* ³²⁴ by inter-scale similarity measurement, respectively. Then we 325 perform the cost aggregation guided by $S_l^{\overline{R}}$ and S_l^T : 326

$$
C_{l}(h', w', d') = \sum_{(h, w, d) \in \mathcal{N}_c} S_{l}^{R}(h', w') S_{l}^{T}(h', w' - d')
$$

$$
C_{l-1}(h, w, d)
$$
. (7) 328

The memory and computational cost of 3D cost aggregation ₃₂₉ are unaffordable. Accordingly, we introduce a decomposition 330 strategy to reduce the computation cost. We split the upsam-
331 pling in full 3D spatial-disparity space into 1D disparity and 332 2D spatial upsampling by leveraging the property of cost vol- ³³³ ume on the disparity dimension. The property is that position 334 (h, w, d) in cost volume represents the (h, w) in the reference 335 image and $(h, w - d)$ in the target image. We warp S_l^T to S_l^R , 336 and then split the mapping of cost volume into 1D disparity 337 dimension and 2D spatial dimension. Specifically, we replace 338 Eq. (7) with a two-step decomposed cost aggregation. 339

In the first step, 1D disparity upsampling, the positions 340 $(h, w, d - \lfloor M/2 \rfloor), \ldots, (h, w, d), \ldots, (h, w, d + \lfloor M/2 \rfloor)$ in $\frac{341}{2}$ cost volume along disparity dimension correspond to (h, w) cost volume along disparity dimension correspond to (h, w) in the reference image and $(h, w - d + |M/2|), \ldots, (h, w - 343)$ *d*), ..., $(h, w - d - |M/2|)$ in the target image. Formally, the 344 updating along the disparity dimension is given by 345

$$
C_l(h, w, d') = \sum_{d \in \mathcal{N}_d} S_l^R(h', w') S_l^T(h', w' - d') C_{l-1}(h, w, d),
$$

$$
(8) \qquad 347
$$

where $\mathcal{N}_d = \{d'/s - \lfloor M/2 \rfloor, \ldots, d'/s, \ldots, d'/s + \lfloor M/2 \rfloor\}.$ 348 In the second step, 2D spatial upsampling, all voxels with ³⁴⁹ location $(h', w', :)$ in cost volume correspond to the pixel with $\frac{350}{250}$

Fig. 3. The overall architecture. Given an image pair, our method extracts multi-scale features at each level *l*. *L* is the total number of levels. \circledR is the warping operation used for generating the initial cost volume in the lowest resolution. \otimes represents element-wise multiplication.

 λ_{351} location (h', w') in the reference image. The update along the ³⁵² spatial dimension is given by

$$
C_l(h', w', d') = \sum_{(h,w)\in\mathcal{N}_{sp}} S_l^R(h', w') C_l(h, w, d'), \qquad (9)
$$

³⁵⁴ where $\mathcal{N}_{sp} \in \mathbb{R}^{\mathbb{M} \times \mathbb{M}}$ is a 2D neighborhood of the pixel with \log_5 location $(h'/s, w'/s)$ at level $l - 1$.

³⁵⁶ After all these operations, we complete the transformation f_{357} from the shape of $H_{l-1} \times W_{l-1} \times D_{l-1}$ to $H_{l-1} \times W_{l-1} \times D_l$ and then to $H_l \times W_l \times D_l$, where $H_l = H_{l-1} \cdot s$, $W_l = W_{l-1} \cdot s$ 359 and $D_l = D_{l-1} \cdot s$.

 3) Loss Function: We use a multi-scale loss function that applies smooth L_1 loss to each level. The smooth L_1 loss function is not sensitive to outliers or noises. The loss function is defined as

$$
D_l = \sum_{d \in (d+1)^N} d \cdot \sigma(-C_l), \qquad (10)
$$

$$
= \sum_{d \in \{d_n\}_{n=1}^N} a \cdot \sigma
$$

$$
\mathcal{L} = \sum_{l} \lambda_l \cdot \mathcal{L}_l (\boldsymbol{D}_l - \boldsymbol{G}_l), \qquad (11)
$$

$$
\mathcal{L}_l(x) = \begin{cases}\n l=0 & \text{if } |x| < 1 \\
 |x| - 0.5 & \text{otherwise}\n\end{cases}
$$
\n(12)

where $\{d_n^l\}_{n=1}^N$ is the disparity hypothesis at level *l*, $\sigma(\cdot)$ is the softmax operation, D_l is the predicted disparity map at level *l*, λ_l denotes the coefficients for the disparity prediction at level σ _{*l*}, and G_l is the ground-truth disparity map at level *l*.

³⁷¹ *C. Computational Cost Analysis*

372 To further demonstrate the superiority of our decomposition strategy in computational complexity, we conducted the fol- lowing analysis and complexity experiments (in Section V). We separate the 3D upsampling into 1D upsampling plus 2D upsampling, reducing the parameters and calculations.

1) Parameters: For deconvolution, the number of param- 377 eters per layer is given by $C \times 1 \times k^3 = Ck^3$, where *k* is 378 the kernel size, C is the number of input channels, and the 379 output channel is set to 1. In contrast, our method requires 380 $Ck²$ parameters per layer. Both our method and deconvolution $\frac{381}{2}$ utilize the same number of layers. 382

2) Calculations: For the computational complexity of 3D ³⁸³ upsampling, comparing 3D deconvolution with our method for 384 a feature volume of size $C \times D \times H \times W$ to be upsampled 385 by a scale of *s*, the computational cost for deconvolution 386 is $\mathcal{O}(s^3k^3)CDHW$, while ours is $\mathcal{O}(s^2k^2 + sk)CDHW = \infty$ $\mathcal{O}(s^2k^2)\mathcal{C}DHW$.

V. EXPERIMENTS 389

A. Datasets 390

1) SceneFlow Dataset: SceneFlow [29] is a large synthetic 39 dataset containing 34896 training images and 4248 testing 392 images with the size of 540×960 . This dataset has three 393 rendered sub-datasets: FlyingThings3D, Monkaa, and Driving. ³⁹⁴ FlyingThings3D is rendered from the ShapeNet dataset and ³⁹⁵ has 21828 training data and 4248 testing data. Monkaa is 396 rendered from the animated film Monkaa and has 8666 training 397 data. The Driving is constructed by the naturalistic, dynamic 398 street scene from the viewpoint of a driving car and has 399 4402 training samples. 400×400

2) KITTI 2015 Dataset: KITTI 2015 [61] is a real-world ⁴⁰¹ dataset with street views from a driving car. It contains ⁴⁰² 200 training stereo image pairs with sparse ground-truth dis- ⁴⁰³ parities obtained using LiDAR and another 200 testing image 404 pairs without ground-truth disparities. During the training pro- ⁴⁰⁵ cess, we take 160 images for training and reference 40 images ⁴⁰⁶ for validation. 407

3) Middlebury-v3 Dataset: Middlebury-v3 is a subset of the 408 2014 dataset $\lceil 62 \rceil$ and is collected in the real world with static $\frac{409}{200}$ indoor scenes containing complicated and rich details. There 410 are 15 stereo pairs for training and 15 stereo pairs for testing. ⁴¹¹ ⁴¹² Each pair is provided in 3 kinds of resolution, full, half, and ⁴¹³ quarter resolution; where we used the quarter resolution in the ⁴¹⁴ experiment.

 4) ETH3D-Two-Iew Dataset: ETH3D (two view) [63] com- prises grayscale stereo pairs captured from diverse indoor and outdoor scenes. The dataset includes 27 training and 20 testing image pairs with sparsely labeled ground truth. Disparities range from 0 to 64 pixels, and bad 1.0 (percentage of pixels with errors larger than 1 pixel) are reported.

⁴²¹ *B. Evaluation Metrics*

c prior grap state pairs are point and the state based of the transformation of the state pairs and the state of th The end-point error (EPE) is the mean disparity error in pixels. The 3-px error refers to the proportion of points in the full map where the absolute value of the differ- ence between the predicted disparity and the true value is greater than 3 pixels. The percentage of disparity outliers in the background (*D1-bg*), foreground (*D1-fg*), or all pixels (*D1-all*) for both noc regions and all regions are applied for evaluation. Disparity outliers are the pixels if their disparity EPE is more than 3 or 5% pixels. *avgerr* is the average absolute error in pixels. *RMS* represents the root mean square of the differences between the estimated and actual disparities. *A90* and *A95* are the 90% and 95% error quantile in pixels, respectively. *Bad 1.0* and *Bad 2.0* percentage of pixels with errors larger than 1 pixel or 2 pixels, respectively.

⁴³⁶ *C. Model Details*

 To prove the effectiveness of our method, we extend five 438 stereo baseline networks with our method, CF-Net [30], HSM-439 Net [7] and PSM-Net [6], FastAcv [44] and FastAcvPlus [44]. All networks are implemented via PyTorch and tested on NVIDIA RTX 3090 GPU. For all baselines, the neighborhood size *M* is set to the scale change *s* at each level.

 For PSM-Net+ours, the model is optimized using Adam [64] with β_1 of 0.9, β_2 of 0.999. During training, the batch size is fixed to 8, and we perform color normalization to each input 446 image and crop them into 256×512 resolution. We train our network on SceneFlow for 10 epochs and change the learning rate from 0.001 to 0.0001 in the 7th epoch. We then fine- tune the network on KITTI 2015 and set the learning rate to 0.001, 0.0001, and 0.00003 in the first 200 epochs, the next 400 epochs, and the final 600 epochs, respectively. As for Middlebury-v3, we also fine-tune the model pre-trained on SceneFlow. The learning rate is set to 0.001 for 300 epochs and then changed to 0.0001 for the rest of 600 epochs. For HSM-455 Net+ours, we use AdamW [65] with β_1 of 0.9, β_2 of 0.999. During training, the batch size is fixed to 12, and we perform ⁴⁵⁷ the same data augmentation [7] of the original HSM-Net and 458 crop the images into 256×512 resolution. We train our network for 10 epochs using the same dataset as HSM-Net and change the learning rate from 0.001 to 0.0001 in the 9th epoch. For CF-Net, FastAcv, and FastAcvPlus, we follow all the training strategies of the official repositories.

Furthermore, we downsample the ground truth for our multi-⁴⁶⁴ scale loss. We use bilinear downsampling in SceneFlow and ⁴⁶⁵ nearest downsampling in KITTI 2015 and Middlebury-v3.

TABLE I EVALUATION RESULTS OF CURRENT STEREO MATCHING ALGORITHMS ON THE SCENEFLOW TEST SET

Model	PSM-Net [6] (2018)	Gwc-Net [13] (2019)	HSM-Net [7] (2019)
EPE(px)	1.09	0.98	2.07
Model	Acf-Net (2020)	LEAStereo (2020)	CF-Net (2021)
EPE(px)	0.87	0.78	0.99
Model	LaC+ GwcNet (2022)	LaC+ GANet (2022)	FastAcv (2023)
EPE(px)	0.75	0.72	0.64
Model	FastAcvPlus (2023)	PSM-Net+ours	HSM-Net+ours
EPE(px)	0.59	0.63	1.39
Model	$CF-Net+ours$	FastAcv + ours	FastAcvPlus + ours
EPE(px)	0.72	0.59	0.57

Additionally, we reduced the computational cost without sacri-
466 ficing accuracy by moving the averaging operation before the 467 aggregation at each layer. Although we observe better results 468 of bilinear downsampling in the experiment on SceneFlow, the ⁴⁶⁹ ground truth disparities of the two real-world datasets contain 470 invalid values, like 0 and INF, which will lead to wrong disparity results after bilinear downsampling. In all experiments, 472 no post-processing or unsupervised learning methods are used. 473

D. Comparison With Stereo Matching Methods ⁴⁷⁴

Our method mainly focuses on recovering the fine-grained 475 details lost during cost volume downsampling. Therefore, ⁴⁷⁶ we conduct experiments on the SceneFlow dataset, specifi-477 cally targeting fine-grained areas, and we compare the results 478 against mainstream baseline methods. Additionally, we per- ⁴⁷⁹ form experiments on real datasets, including KITTI and ⁴⁸⁰ Middlebury, to validate the effectiveness of our approach. 481

1) SceneFlow: The experimental results in Table I ⁴⁸² show that our proposed method significantly improves 483 the performance of stereo matching algorithms, with the ⁴⁸⁴ FastAcvPlus+ours achieving the lowest EPE of 0.57. The consistent reduction in EPE across various models demonstrates 486 the robustness and efficacy of our method. 487

a) Fine-grained areas: We test different baselines in the 488 fine-grained region on the SceneFlow dataset to verify the 489 accuracy improvement of our method in the fine-grained (FG) ⁴⁹⁰ areas and full areas, as shown in Table II . We use the calculated 491 HOG [66] descriptor of the reference image as a mask of finegrained areas. The results in Table II show the superiority of 493 our method in fine-grained areas. Our method can improve ⁴⁹⁴ the accuracy significantly in fine-grained areas, and 37.6%, ⁴⁹⁵ 32.9%, 16.2%, 11.4% and 10.4% EPE reduction in PSM-Net, ⁴⁹⁶ HSM-Net, CF-Net, FastAcv and FastAcvPlus, respectively. ⁴⁹⁷ Our method is effective for different baselines with good ⁴⁹⁸ universality. Our method also brings no or small increase in ⁴⁹⁹ runtime. For PSM-Net, we remove the time-consuming 3D 500 convolution layers in the hourglass modules at RES 1/16 and 501 RES 1/8. For the rest baselines, we directly plug our method 502 into them without additional model modification. 503

The visualization results for the fine-grained regions are 504 depicted in Fig. 4. Our method successfully recovers more 505 details, notably improving estimation results for fine-grained 506 areas like the spokes of the wheel and plant spikes in the 507 left column of Fig. 4 compared to the baseline. Furthermore, $\frac{508}{200}$ our approach enhances results in less refined regions, such as $_{509}$ inside the bounding box in the right column of Fig. $4.$ 510

TABLE II

RESULTS OF DIFFERENT BASELINE IN FULL AREAS (FULL) AND FINE-GRAINED (FG) AREAS ON THE SCENEFLOW DATASET. FOR PSM-NET, WE REMOVE THE TIME-CONSUMING 3D CNNS AT RES 1/16 AND RES 1/8

Method	EPE in Full	EPE in FG	Time (s)
PSM-Net [6] (2018)	1.09	1.01	0.41
PSM-Net+ours	0.60	0.63	0.37
HSM-Net [7] (2019)	1.88	2.07	0.05
HSM-Net+ours	1.25	1.39	0.09
CF-Net [30] (2021)	1.06	0.99	0.18
CF-Net+ours	0.72	0.83	0.22
FastAcv [44] (2023)	0.64	0.70	0.05
FastAcv+ours	0.59	0.62	0.08
FastAcvPlus [44] (2023)	0.59	0.67	0.05
FastAcvPlus+ours	0.57	0.60	0.08

Fig. 4. The results of PSM-Net [6] and PSM-Net+ours on the SceneFlow dataset.

 b) Full areas: Our method brings improvement for full areas across different baselines. Visualization of the results (Fig. 5) reveals that our method exhibits certain corrective effects on large-scale weakly-textured regions as well. The experimental results demonstrate that our approach achieves significant accuracy improvement when applied to datasets with complete depth information as ground truth.

 2) Kitti: Table III displays the performance and runtime of various algorithms evaluated on the KITTI stereo2015 benchmark. Across different baselines, our method enhances the accuracy of the original baselines with only a marginal increase in processing time. Notably, CF-Net combined with our method surpasses other competing methods in the Noc D1-all and All D1-all. Next, we would like to provide a more detailed explanation of the comparison between our method and stereo matching methods based on attention mechanisms, as well as methods based on decomposition strategies.

TABLE III

a) Compared with the attention-based method: HDA- ⁵²⁸ Net [67] proposes an efficient horizontal attention module 529 to adaptively capture the global correspondence clues. Our 530 method uses inter-scale information to generate similarity 531 guidance to improve cost aggregation. As shown in Table III , 532 our method has lower D1-all (HDA-Net 2.03 *vs.* CF-Net+Ours 533
1.87) with faster running time (HDA-Net 0.42ms *vs.* 534 1.87) with faster running time (HDA-Net 0.42ms *vs.* $CF-Net+Ours$ 0.22ms) on the KITTI 2015 dataset.

b) Compared with the decomposition method: DecNet 536 [31] decomposes the original stereo matching into a dense 537 matching at the lowest resolution and a series of sparse 538 matching at higher resolutions. Unlike DecNet, our method 539 decomposes the 3D upsampling of cost volume into a 2D- ⁵⁴⁰ spatial and 1D-disparity upsampling. Our method outperforms $_{541}$ DecNet in D1-all (Dec-Net 2.37 *vs.* HSM-Net+Ours 2.09) 542 but is slower in runtime (Dec-Net 0.05ms *vs.* HSM-Net+Ours 543 0.09 ms), as shown in Table III. 544

c) Visualization: Fig. 6 presents the experimental results 545 on the KITTI 2015 dataset, showcasing images from top to ⁵⁴⁶ bottom. Our method excels in recovering slender structures, 547 as seen in the iron chain at the center of the first row and ⁵⁴⁸ the fence in the lower left corner of the third row. Moreover, ⁵⁴⁹ our approach accurately estimates depth-mutation areas such 550 as signboards and utility poles. For instance, unlike PSM-Net 551 and HSM-Net in the first row's bounding box around the 552 signboard, our method produces correct results. In rows two, 553 five, and six, the other methods misidentify parts of the 554 background as utility poles, which our method avoids. 555

3) Middlebury: We compare our method with several 556 approaches using different aggregation strategies on the 557 Middlebury stereo dataset v3, as shown in Table IV. We out-

₅₅₈ perform these 3D aggregation based approaches on most of $\frac{559}{2}$ the metrics. The result also demonstrates the effectiveness of $\frac{560}{200}$ our content-aware upsampling method. Based on the visual- ⁵⁶¹ izations in Fig. 7, we can draw the following conclusions: ⁵⁶² 1) Improved depth estimation for fine-grained regions: ⁵⁶³ Our method shows superior performance in depth estima- ⁵⁶⁴ tion for fine-grained regions, demonstrating the effectiveness 565 of explicitly integrating high-resolution and low-resolution ⁵⁶⁶ information. This is evident in almost all cases, such as the 567

Fig. 5. The visualization of results on HSM-Net baseline. The first and second columns are the reference input images and ground truth. The rest columns are results from HSM-Net and HSM-Net+ours.

Fig. 6. The results of different deep stereo networks on KITTI 2015 dataset. Our method performs better in fine-grained areas than other methods, especially for the region denoted with the boxes. Please zoom in to check the details.

 detailed areas in "DjembL" and the water cup on the table in "Crusade" (Line 3, PSM-Net vs. PSM-Net + ours), as well as the small figurine (Line 3, HSM-Net vs. HSM-Net + ours).
 571 2) Enhanced foreground and background decoupling: Our 2) Enhanced foreground and background decoupling: Our method has a stronger ability to decouple the foreground from the background. Retaining low-resolution information effec- tively enhances this capability. Examples include the depth estimation of the potted plants and background in "Plants" (Line 5) and the estimation of the hollow part of the staircase handrail in "Staircase" (Line 4, HSM-Net vs. HSM-Net + ours; CF-Net vs. CF-Net + ours). 3) Competitive perfor- mance in flat regions: Our method also shows competitive performance in flat regions. For instance, the wall in the upper left of "Staircase" (Line 4, PSM-Net vs. PSM-Net + ours) and the restoration of the table corner in "Crusade" (Line 3, ⁵⁸² $CF-Net$ vs. $CF-Net + ours$). However, our method has some 583 shortcomings in certain areas, such as the seats in the PSM-Net 584 case of "Classroom2E" (Line 1, PSM-Net vs. PSM-Net $+$ 585 ours). We will systematically discuss these limitations in the 586 Limitation Analysis section. 587

E. Ablation Studies 588

We conduct all the analysis in ablation studies mainly on 589 the HSM-Net baseline. Ablation studies are performed on the 590 SceneFlow dataset and the KITTI 2015 dataset.

1) Effectiveness of Stereo-Content-Aware Cost Aggregation: ⁵⁹² During Stereo-Content-Aware Cost Aggregation, we use both 593

Fig. 7. The visualization of results on Middlebury-v3 test set. In the first column are the reference input images. The rest columns are results from PSM-Net $[6]$, PSM-Net + ours, HSM-Net $[7]$, + ours, CF-Net $[30]$ and CF-Net + ours respectively.

TABLE IV EVALUATION ON MIDDLEBURY-V3. THE BEST RESULTS FOR EACH EVALUATION METRIC ARE SHOWN IN BOLD

Models	Res.	Avgerr	Rms	A90	A95
PSM-Net ROB (2018) [6]	О	8.78	23.3	22.8	43.4
DeepPruner (2019) [68]	Ω	6.56	18	17.9	33.1
FADNet++ (2021) [69]	O	11.9	27.7	34.3	61.2
MCP-HA-VO (2022) [70]	O	6.01	37.5	40.6	85.9
H-CENST (2022) [71]	O	10.2	29.1	24.3	59.0
FM-DT (2023) [72]	O	11.7	31.4	33.4	67.1
PSM-Net+ours		5.43	17.3	8.11	25.2

 reference and target images to extract similarity guidance and separate the 3D spatial-disparity upsampling into 1D dispar- ity / 2D spatial upsampling. We evaluate the effectiveness of our method at different resolutions through two experiments: i. Training on the SceneFlow dataset and testing on the SceneFlow dataset. ii. Training on the SceneFlow dataset and testing on the validation set of the KITTI 2015 dataset. Table V demonstrates that our decomposition strategy reduces the running time by nearly half compared to full 3D upsampling at the setting of "RES 1/16 to RES 1/8" and "RES 1/8 to RES 1" on the SceneFlow dataset and KITTI 2015 dataset. Our decomposition strategy not only proves to be faster but also more accurate than full 3D upsampling. When integrating our method at "RES 1/16 to 1/8," HSM-Net+ours experiences a decrease in EPE of 18.09% and 15.86% compared to the original HSM-Net on the SceneFlow dataset and the KITTI 2015 dataset, respectively. Plugging our method at higher resolutions, i.e., "RES 1/8 to 1", the EPE of HSM-Net+ours is 33.51% and 26.21% lower than the original HSM-Net on the SceneFlow dataset and the KITTI 2015 dataset, respectively. Our method is effective and the higher the resolution at which 615 we employ our method, the greater the improvement it brings.

2) Effectiveness of Inter-Scale Similarity Measurement: ⁶¹⁶ We utilize inter-scale similarity measurement to generate a_{617} similarity guidance map for cost aggregation. Each pixel in the 618 similarity map corresponds to the content information at the 619 same location. Our method calculates the similarity between 620 high-resolution feature points and their corresponding $M \times M$ 621 points in the low-resolution counterpart. Visualizations of 622 similarity maps of a 3 size neighborhood are shown in Fig. $8.$ 623

We confirm the effectiveness of our inter-scale policy on 624 the SceneFlow dataset through a series of experiments. These 625 experiments are conducted in three settings: without similarity guidance, with single-scale similarity guidance, and 627 with inter-scale similarity guidance. The results presented 628 in Table VI clearly demonstrate that the use of inter-scale 629 similarity guidance results in higher accuracy when com- 630 pared to single-scale similarity guidance. The inter-scale 631 similarity guidance transforms the unary mapping inherent 632 in single-scale similarity guidance into a pair-wise map- ⁶³³ ping, consequently leading to improved accuracy. Furthermore, ⁶³⁴ we verify the significance of employing stereo information, 635 which includes both reference and target images, to achieve 636 favorable results. In Table VI , it is evident that the EPE when 637 using stereo information is significantly lower than when not 638 using stereo information. Utilizing stereo information to model 639 the mapping relationship between cost volumes of different 640 resolutions proves to be more reliable than relying solely on 64 reference images. 642

3) Effectiveness of Our Method in Different Resolution: ⁶⁴³ We further provide visualizations of the results obtained from 644 HSM-Net and HSM-Net+ours at different resolutions on the 645 SceneFlow dataset. These visualizations help us understand 646 how our model enhances the baseline at various resolutions, 647 as shown in Fig. 9. At a resolution of 1/32, HSM-Net 648

RESULTS OF USING THE GUIDANCE IN MULTIPLE STEPS OF MULTI-SCALE COST AGGREGATION ON SYNTHETIC AND REAL DATASETS. RES 1/16, 1/8, 1 REPRESENTS THE ORIGINAL IMAGE'S 1/16, 1/8, AND 1 RESOLUTION. RES 1/16 TO 1/8 INDICATES WHETHER THE BASELINE IS PLUGGED WITH OUR METHOD IN COST AGGREGATION FROM RESOLUTION 1/16 TO RESOLUTION 1/8, SO AS RES 1/8 TO 1

TABLE V

Fig. 8. The visualization of similarity. (a) and (b) are the similarity of the two images. The three columns on the right are visualizations of the similarity, representing the similarity of points in high resolution to their corresponding neighbors in low-resolution projection points. In each map, the brightness indicates the similarity, which corresponds to the upsampling kernel weight. It can be seen that the aggregation weight is directly related to the image content and that each weight in the global picture uniquely adapts the content information of the corresponding points.

TABLE VI

THE RESULTS OF USING DIFFERENT SCALES OF GUIDANCE TO GUIDE COST AGGREGATION. "INTER-SCALE" AND "SINGLE-SCALE" REP-RESENT THAT THE GUIDANCE MAPS ARE GENERATED FROM ADJACENT SCALES OR A SINGLE SCALE, RESPECTIVELY. THE "STEREO INFO" INDICATES WHETHER THE GUIDANCE MAPS ARE GENERATED WITH STEREO INFORMATION INCLUDING BOTH REFERENCE AND TARGET IMAGE FEATURES, OR ONLY FEATURES OF THE REFERENCE IMAGES

 exhibits a failure in recovering the objects within the white bounding box, but our method successfully rectifies this error. Additionally, our method corrects the gaps within the blue bounding box at a resolution of 1/16. From a resolution of 1/32 to 1, our method effectively recovers the triangular area within the black bounding box. It is evident that high-resolution cost aggregation is markedly influenced by low-resolution cost aggregation. Our method systematically addresses errors in the original method at each resolution, commencing with the lowest resolution.

⁶⁵⁹ *F. Generalization Evaluation*

⁶⁶⁰ *1) Universality of Cost Aggregation Method on Different* ⁶⁶¹ *Baseline:* We apply our method to five stereo networks, i.e.,

PSM-Net [6], HSM-Net [7], and CF-Net [30], FastAcv [44] 662 and FastAcvPlus [44] to verify the university of our method. 663 The results on the SceneFlow dataset are shown in Table II , 664 and the results on the KITTI 2015 dataset are shown in 665 Table III. 666

For PSM-Net, HSM-Net, and CF-Net, our methods have 667 improved by 44.5% , 33.5% , and 32.1% on the SceneFlow 668 dataset, respectively. Moreover, our method has achieved 669 reductions in D-all metrics for all three baselines on the 670 KITTI 2015 dataset. Our method consistently enhances various 671 baselines on both synthetic and real datasets. 672

2) Zero-Shot Generalization Ability: Obtaining large-scale 673 real-world datasets for training is challenging, making the ⁶⁷⁴ generalization capability of stereo models crucial. To this end, 675 we evaluate the generalization performance of our methods 676 from synthetic datasets to unseen real-world scenes. In this 677 evaluation, we train various baseline models augmented with 678 our approach on the Scene Flow dataset and directly evaluate 679 them on the Middlebury 2014 and ETH3D training sets. 680 As shown in Table VII, our method consistently outper- 681 forms all baselines, demonstrating its strong generalization 682 capability.

G. Comparison With Content-Aware Upsamping Methods ⁶⁸⁴

To demonstrate our superiority over conventional ⁶⁸⁵ content-aware upsampling operators, we directly applied 686 $CARAFF++$ [59] to the HSM-Net baseline for comparative $\frac{687}{687}$
analysis. The content-aware operators were implemented $\frac{687}{688}$ analysis. The content-aware operators were implemented at resolutions of $\frac{1}{32}$, $\frac{1}{16}$, and $\frac{1}{8}$ of full resolution, aligning 689

Fig. 9. Results of HSM-Net and HSM-Net+ours at different resolutions. We obtain the disparity map by regressing the cost volume at each resolution.

 with the settings of our method. We conducted training and testing of HSM-Net with CARAFE++ on the SceneFlow dataset, using EPE as the measurement metric. The results presented in Table VIII clearly indicate that our method outperforms CARAFE $++$ in terms of accuracy and speed. Inter-scale information provides us with a broader speed. Inter-scale information provides us with a broader receptive field for aggregation and access to more content information. Furthermore, our approach involves separating the 3D upsampling process into 1D and 2D upsampling, resulting in a significant reduction in computational ⁷⁰⁰ cost.

1) Complexity Analysis: To further demonstrate the supe- 701 riority of our decomposition strategy in computational ⁷⁰² complexity, we conducted the following analysis and com- ⁷⁰³ plexity experiments. We separate the 3D upsampling into ⁷⁰⁴ 1D upsampling plus 2D upsampling, reducing the parameters 705 and calculations. We test the memory cost of different cost 706 aggregation methods of HSM-Net in $\frac{1}{8}$ and 1 of the full $\frac{707}{207}$ resolution (540 \times 960) of the SceneFlow dataset and the results τ ₀₈ are shown in Table IX. At the same resolution, our module 709 exhibits lower memory and time consumption compared to $\frac{710}{200}$ the other two upsampling methods. $\frac{711}{200}$

TABLE VII TABLE IX SYNTHETIC TO REAL GENERALIZATION EXPERIMENTS. ALL MODELS ARE TRAINED ON SCENE FLOW. THE BAD 2.0 ERROR RATE IS USED FOR MIDDLEBURY-V3, AND THE BAD 1.0 ERROR RATE

FOR ETH3D

TABLE VIII

RESULT OF COMPARISON BETWEEN CARAFE++ [59] AND OURS IN BASELINE HSM-NET [7]. BOTH CARAFE++ AND OURS ONLY REPLACE THE UPSAMPLING MODULE AT RES 1/16 TO 1/8

TABLE IX

(COMPLEXITY AND EFFICIENCY ANALYSIS OF DIFFERENT COST AGGRE-GATION STRATEGIES (THE BASELINE MODEL IS HSM-NET). DUE TO HARDWARE LIMITATIONS, WE DO NOT RUN CARAFE++ AT 1/8 TO 1 RESOLUTION. THE BEST RESULTS FOR EACH EVALUATION METRIC ARE SHOWN IN BOLD

⁷¹² *H. Limitation*

 1) Lack of Dense Outdoor Data: The performance gains for outdoor scenes are smaller compared to those in virtual and indoor datasets. Additionally, in the CF-Net baseline, our method still fails to completely correct the erroneous depth estimation for the sky, as shown in Fig. 10 (a). We believe there are two main reasons for this: 1) Poor ground truth quality. Outdoor datasets like KITTI use LiDAR scanning, resulting in sparse depth maps. Ground truth is missing in areas beyond the LiDAR scan range, as shown in Fig. 10 (b). This sparsity affects model training. 2) Lack of fine-grained regions. Our method focuses on fine-grained areas, but the coarse nature of LiDAR scans in outdoor datasets means many details are overlooked. For this scenario, we believe that employing some advanced depth completion methods to refine sparse areas in the ground truth could be a reasonable approach.

⁷²⁸ *2) Future Work:* In future work, we aim to delve into ⁷²⁹ super-resolution techniques to augment the detail information

Fig. 10. Failure case and ground-truth in the outdoor scenarios.

within extensive textureless areas, which will significantly 730 bolster the performance in outdoor environments. Furthermore, $\frac{731}{2}$ the present study has adopted a distinct spatial domain mod- ⁷³² eling strategy to address the issue of detail loss. Yet, the 733 utilization of high-frequency components in the frequency ⁷³⁴ domain for such fine-grained information presents itself as 735 an inherently viable alternative. Moving forward, we intend 736 to experiment with frequency domain analysis techniques, 737 including wavelet transformations, to facilitate the restoration 738 of fine-grained regional information.

VI. CONCLUSION 740

We have presented an inter-scale similarity guided cost $_{741}$ aggregation method designed to adaptively recover details $_{742}$ in fine-grained areas. By leveraging both low-resolution ⁷⁴³ and high-resolution information, our approach effectively $_{744}$ exploits detail while generating inter-scale similarity measure- ⁷⁴⁵ ments. Additionally, our stereo-content-aware cost aggregation $_{746}$ method employs a decomposition strategy that divides the 3D $\frac{747}{640}$ disparity-spatial space into 1D disparity space and 2D spatial ⁷⁴⁸ space, significantly reducing computational costs associated 749 with 3D cost volumes. Experimental results across three 750 benchmarks demonstrate the effectiveness of our method with 751 various models. 752

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Inter-Scale Similarity Guided Cost Aggregation for Stereo Matching

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Abtence.—Sterio matching sina to estimate 3D geometry by The well-known priging divides acress matching

is computed description a *Abstract*— Stereo matching aims to estimate 3D geometry by computing disparity from a rectified image pair. Most deep learning based stereo matching methods aggregate multi-scale cost volumes computed by downsampling and achieve good performance. However, their effectiveness in fine-grained areas is limited by significant detail loss during downsampling and the use of fixed weights in upsampling. In this paper, we propose an inter-scale similarity-guided cost aggregation method that dynamically upsamples the cost volumes according to the content of images for stereo matching. The method consists of two modules: inter-scale similarity measurement and stereo-content- aware cost aggregation. Specifically, we use inter-scale similarity measurement to generate similarity guidance from feature maps in adjacent scales. The guidance, generated from both reference and target images, is then used to aggregate the cost volumes from low-resolution to high-resolution via stereo-content-aware cost aggregation. We further split the 3D aggregation into 1D disparity and 2D spatial aggregation to reduce the computational cost. Experimental results on various benchmarks (e.g., Scene- Flow, KITTI, Middlebury and ETH3D-two-view) show that our method achieves consistent performance gain on multiple models (e.g., PSM-Net, HSM-Net, CF-Net, FastAcv, and FactAcvPlus). The code can be found at https://github.com/Pengxiang-Li/issga-²⁴ stereo.

²⁵ *Index Terms*— Stereo matching, cost aggregation, content-²⁶ aware upsampling.

27 **I. INTRODUCTION**

28 STEREO matching aims to estimate a pixel-wise dis-
29 parity map from a rectified image pair. It plays an
important role in verious emplications including 2D room. ³⁰ important role in various applications including 3D recon-31 struction [1], AR [2], SLAM [3], and autonomous driving [4].

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The well-known pipeline divides stereo matching into four 32 steps: cost computation, cost aggregation, disparity computa-
33 tion, and disparity refinement [5]. Among these four steps, 34 cost aggregation plays a pivotal role in leveraging neighbor- ³⁵ hood information to rectify the ambiguous matching costs in 36 ill-posed regions such as occluded regions, large textureless 37 areas, repetitive patterns, and thin structures. The cost aggre- ³⁸ gation is commonly embedded into end-to-end deep neural 39 networks with multi-scale processing to enlarge the receptive 40 field. 3D CNNs [6], [7], GRU [8], [9], and attention mecha- ⁴¹ nism [10] are the most commonly used basic structures for cost 42 aggregation, effectively correcting ambiguous matching costs 43 and substantially enhancing prediction accuracy in ill-posed ⁴⁴ regions by aggregating multi-scale cost volumes.

However, these cost aggregation methods often struggle in 46 fine-grained areas due to considerable detail loss during down- ⁴⁷ sampling and fixed weight used in upsampling. Many efforts 48 have been targeted at improving the performance of stereo 49 matching in fine-grained areas, including edge information 50 [11], deformable convolutions [12], group-wise correlation 51 [13] and slanted planes [14]. These methods have achieved 52 good performance, but two challenging problems in cost 53 aggregation are still not well solved: (1) the downsampling 54 causes considerable detail loss during the construction of ⁵⁵ multi-scale cost volumes, and (2) the upsampling fixed in size $\frac{56}{60}$ and weight is prone to data imbalance between large-smooth 57 areas and fine-grained areas. For example, the HSM-Net [7] 58 with multi-scale cost volumes and upsampling fixed in size and 59 weight may lead to poor performance in fine-grained areas, $\overline{60}$ as illustrated in Fig. 1 (b) and Fig. 1 (c). $\qquad \qquad \text{61}$

In this paper, we propose inter-scale similarity-guided cost 62 aggregation that adaptively restores image details by dynam- 63 ically upsampling cost volumes based on image content. ⁶⁴ Our method comprises two modules: inter-scale similar- ⁶⁵ ity measurement and stereo-content-aware cost aggregation. 66 We utilize inter-scale similarity measurements to generate 67 similarity guidance from the feature maps of adjacent scales. 68 Subsequently, we employ this guidance to aggregate the 69 multi-scale cost volumes through stereo-content-aware cost 70 aggregation.

For the first challenging problem, our idea is to retrieve $\frac{72}{2}$ the fine-grained details lost during the downsampling pro- ⁷³ cess. We use inter-scale similarity measurement to measure $\frac{74}{6}$ the similarity between high-resolution and low-resolution 75 features. The similarity explicitly preserves the connection ⁷⁶ between high-resolution details and low-resolution features, 77

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Fig. 1. Predictions and upsampling weights visualizations of HSM-Net [7] using different upsampling strategies.

 thereby providing guidance for the upsampling process to restore details. Technically, we first project a point *xhigh* from high-resolution to low-resolution features *xlo*w. Then 81 we compute the similarity between the point in the high- α resolution x_{high} and the neighbors of the projected point in low-resolution N*lo*w.

 For the second challenging problem, a critical factor leading to the suboptimal restoration of fine-grained details is the fixed size and weights of existing upsampling strategies, 87 which are unable to adapt to the complicated fine-grained details. Motivated by this, we replace the fixed upsampling with content-aware upsampling. The content-aware upsam- pling uses the content information of each point to guide the upsampling process, thereby mitigating the impact of data imbalance between large-smooth and fine-grained areas. 93 In stereo-content-aware cost aggregation, we use similarity guidance (generated from both reference and target images) to guide the aggregation of matching costs in 3D spatial-disparity space. The pair-wise 3D upsampling is computationally expen- sive. Thus, we split the upsampling in the 3D space into 1D disparity and 2D spatial space. As a result, our method is able to efficiently and adaptively assemble the proper neighbors for cost aggregation and upsampling. Our method generates upsampling weight according to the image content and achieves much finer details, as shown in Fig. 1 (d). Our method can be plugged into any multi-scale cost volume based stereo network and achieve higher accuracy, especially in fine-grained areas.

¹⁰⁶ Our contributions are summarized as follows:

¹⁰⁷ 1) We propose an inter-scale similarity guided cost aggre-¹⁰⁸ gation method to adaptively recover the details of cost volumes under the guidance of similarity generated from 109 images. 110

- 2) We introduce an inter-scale similarity measurement to 111 dynamically generate guidance by incorporating infor- ¹¹² mation from both low-resolution and high-resolution 113 feature maps. The explicit utilization of high-resolution ¹¹⁴ feature maps ensures the preservation of fine-grained 115 details. 116
- 3) We design a decomposition strategy that splits 3D 117 disparity-spatial upsampling into 1D disparity and 2D 118 spatial upsampling, significantly reducing the computa-
119 tional cost of the 3D pair-wise upsampling.

II. RELATED WORK 121

A. Stereo Matching 122

Traditional stereo matching methods estimate disparity ¹²³ maps for rectified image pairs using local [15], [16], 124 global [17], [18], and semi-global methods [19], [20], [21]. ¹²⁵ Deep learning-based stereo matching networks now dominate, 126 delivering state-of-the-art results. Early deep learning methods 127 replaced steps in stereo matching [5]: cost computation [22], $_{128}$ [23], [24], cost aggregation [25], [26], [27], disparity compu- ¹²⁹ tation $[28]$, and disparity refinement $[26]$, $[27]$. Despite good 130 performance, their non-end-to-end approaches limited data 131 utilization. To overcome this, end-to-end methods compute 132 correlations by warping the target image to the reference 133 image $[8]$, $[9]$, $[11]$, $[29]$. These achieve excellent results but $_{134}$ often lose geometric information. Cost-volume-based mod- ¹³⁵ els [6], [30], [31], [32], [33], [34], [35] preserve geometric ¹³⁶ information by concatenating multi-scale cost volumes. State- ¹³⁷ of-the-art methods use convolution neural networks [36], [37], ¹³⁸ [38], [39], [40], [41] or attention mechanisms [10], [42], [43], 139 [44] to aggregate these volumes, effectively utilizing image 140 context information. 141

However, multi-scale cost volume-based stereo matching 142 methods often lose fine-grained details due to downsampling. 143 While cost aggregation usually recovers these details, current 144 fixed-size and fixed-weight schemes struggle with data imbal- ¹⁴⁵ ances between large smooth, and fine-grained areas. To address 146 this, we developed a content-aware cost aggregation method ¹⁴⁷ that mitigates detail loss during multi-scale cost volume cre- ¹⁴⁸ ation. Our adaptive upsampling approach also remains robust ¹⁴⁹ against data imbalances. 150

B. Cost Aggregation 151

Multi-scale cost aggregation methods [6], [29] enhance 152 matching cost reliability by optimizing multi-scale cost volumes for precise disparity estimation. Song et al. [11] used 154 edge information to guide cost aggregation, reducing edge mis- ¹⁵⁵ matches. Zhang et al. [45] improved efficiency by replacing 3D 156 CNNs with semi-global aggregation. Yang et al. [7] proposed a 157 hierarchical feature volume decoder for high-resolution image 158 disparity estimation. Xu et al. [12] utilized deformable con- ¹⁵⁹ volution for adaptive aggregation. Lipson et al. [8] designed 160 an iterative mixed disparity sampling and aggregation strategy. ¹⁶¹ Liu et al. [46] used local features to address over-smoothing. 162 Zhang et al. [47] introduced depth-based sampling for bal- anced density in close and far regions. Xu et al. [48] utilized bilateral grid processing for faster aggregation. Lee et al. [49] introduced a cluster-wise cost aggregation algorithm to paral-lelized scanline-level disparity computation.

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manual variable can be formulated. The generation of the control of the
state in the state of the state of the state of the state of the state of
 α in the state of the state in the state The aforementioned methods demonstrate commendable performance, even in ill-posed areas. However, they still suffer from the loss of details in downsampling, and their strategies for multi-scale cost aggregation are susceptible to data imbalance. These strategies commonly rely on either bilinear interpolation or deconvolution for upsampling. Both bilinear interpolation and deconvolution employ a fixed inter- polation rule or deconvolution kernel across all data points, thus failing to exploit the content information of images fully. Constrained by computational memory limitations, these methods are unable to perform direct aggregation at full resolution. Instead, they resort to upsampling to full resolution without introducing additional parameters after aggregat- ing at 1/2 or 1/4 resolution. However, relying solely on parameter-free upsampling is inadequate for recovering lost ¹⁸³ details.

¹⁸⁴ *C. Upsampling*

 Upsampling is used to transform data from low-resolution to high-resolution. Traditional upsampling strategies fit a curve of a small neighborhood of the upsampled points to com- pute values for interpolated points, including nearest neighbor interpolation [50], bilinear interpolation [51], trilinear interpo- lation [52], and bicubic interpolation [53], etc. The advantage of these methods lies in their low computational cost. How- ever, these parameter-free upsampling strategies underutilize image content, resulting in blurred recovery results in fine- grained areas. Deconvolution [54], [55], [56], [57] offers a learning-based approach to upsampling, where weights are optimized through backpropagation. Learning-based upsam- pling kernels enable the utilization of contextual information learned from extensive data. However, deconvolution has lim- itations as it struggles in various scenes due to fixed kernel sizes and weights, making it susceptible to data imbalances.

 Several works [58], [59], [60] use content-aware upsampling operators to solve the fixed-weight problem. Wang et al. [58], [59] presented a content-aware reassembly approach and argued that traditional feature upsampling methods struggle to capture rich semantic information. While content-aware upsampling mitigates the fixed-weight problem, it relies solely on information from the low-resolution side (i.e., the upsam- pling process could be regarded as a unary low-resolution to high-resolution mapping). However, the upsampling process inherently consists of both low-resolution and high-resolution components, and relying solely on low-resolution features for upsampling may not suffice. Instead of employing a unary upsampling mapping, we introduce an inter-scale similarity measurement approach to produce a pair-wise upsampling mapping, represented by similarity guidance derived from information gathered across adjacent scales. In other words, we actually model the upsampling process as a binary mapping between low-resolution and high-resolution.

III. OPTIMIZATION IN MULTI-SCALE COST AGGREGATION 219

In this section, we model the optimization objectives for 220 each layer of multi-scale cost aggregation. Given a cost volume 221 $C_{l-1} \in \mathbb{R}^{H_{l-1} \times W_{l-1} \times D_{l-1}}$ at level $l-1$ as input, C_l is computed 222 via a network with learning weights W_l . The generation of C_l 223 can be formulated as 224

$$
p(C_l) = p(C_l|C_{l-1}, W_l)p(W_l)p(C_{l-1})
$$

$$
=p(C_l|C_{l-1},W_l)p(W_l). \qquad (1) \quad \text{226}
$$

The probability $p(C_l)$ of cost volume is commonly computed 227 by $p(C_l)$ = softmax($-C_l$), and $p(C_{l-1})$ is supposed to be 1 as 228 C_{l-1} has already been given. Then, the optimization objective 229 is to find the best W_l , that recovers the details lost in C_{l-1} , 230 is to find the best W_l that recovers the details lost in C_{l-1} , which can be formulated as 231

$$
W_l = \underset{W_l}{\operatorname{argmax}} \ p(W_l | C_l, C_{l-1}), \tag{232}
$$

$$
= \underset{W_l}{\text{argmax}} \ p(W_l|C_l), \tag{233}
$$

$$
= \underset{W_l}{\text{argmax}} \ \frac{\text{p}(C_l|W_l) \cdot \text{p}(W_l)}{\sum_{W_l} \text{p}(C_l|W_l)\text{p}(W_l') dW_l'}, \qquad \qquad \text{234}
$$

$$
\stackrel{a.s.}{=} \underset{W_l}{\text{argmax}} \ \ p(C_l|W_l) \cdot p(W_l), \tag{235}
$$

$$
\stackrel{a.s.}{=} \operatorname*{argmax}_{W_l} p(C_l). \tag{2}
$$

In the aforementioned cost aggregation process, it becomes 237 impractical to recover the details lost during downsampling 238 using bilinear upsampling or deconvolution. This is because 239 *W*_l is optimized by cost volumes at level $[0, 1, \ldots, l-1]$, and 240 it doesn't consider the image content at level *l*. In other words, ²⁴¹ only minimal details at level l contribute to the optimization of $_{242}$ W_l . Furthermore, the kernel weights are influenced by the content that appears more frequently in the image. Consequently, ²⁴⁴ it becomes challenging to utilize these fixed kernel weights ²⁴⁵ effectively for recovering details that constitute only a small ²⁴⁶ proportion of the image content such as the fine-grained areas. ²⁴⁷

IV. PROPOSED METHOD ²⁴⁸

A. Problem Formulation ²⁴⁹

Detail loss and biased upsampling are two challenging ²⁵⁰ problems that cause poor performance in fine-grained areas. ²⁵¹ To address these two problems, we optimize cost aggregation 252 with image features at levels *l* and *l* − 1. In our method, 253 the optimization objective of cost aggregation at each level 254 is given by ²⁵⁵

$$
W_l = \underset{W_l}{\operatorname{argmax}} \, \mathrm{p}(C_l) \cdot \mathrm{p}(W_l | F_l, F_{l-1}), \tag{3}
$$

where F_l is the feature map at level *l*.

In particular, the optimization objective of cost aggregation 258 with deconvolution is actually one special case of ours, where 259 $p(W_l|F_l, F_{l-1}) = p(W_l)$. Besides, the optimization objective 260 of cost aggregation with bilinear interpolation is one special ²⁶¹ case of deconvolution, i.e., Eq. (2). With substituting $p(W_l) =$ 262 1 into Eq. (2) , Eq. (2) can be reformulated as 263

$$
W_l = \underset{W_l}{\text{argmax}} \ p(C_l), \tag{4}
$$

Fig. 2. The visualization of aggregation weight and disparity distribution in cost volume. The upper row shows the aggregation weight and the under row shows the distribution of the cost volume along the disparity dimension for a single point. The point in each distribution map is the ground truth for the point in the reference image. Both the bilinear upsampling and deconvolution predict wrong results, while ours not only predicts the correct disparity but also corrects for multi-modality in the distribution.

²⁶⁵ which is just the optimization objective of cost aggregation ²⁶⁶ with bilinear interpolation.

Where (N, u^2) and (n, u) are the bosnion at high-

low-degree control of (n, u^2) and (n, u) are the bosnion at high-

low-degree procedures on the disperties of the set of N , N , C is the set of the set of the set $_{267}$ In our method, W_l is automatically adjusted from the 268 change of F_l and F_{l-1} during inference, whereas the weights of deconvolution or bilinear interpolation remain static. Our method generates aggregation weight related to the image content and achieves unimodal distribution results, while oth- ers get multimodal distribution or wrong distribution. Fig. 2 provides a visual representation of aggregation using various upsampling strategies. As shown in Fig. 2, the weights for bilinear interpolation remain constant, the weights for decon- volution are repetitive kernels, while our method's weights are content-aware, closely linked to the image's content. It's also worth noting that our method effectively addresses the issue of multiple peaks in the disparity distribution (see the distribution curves of Deconvolutions vs. Ours in Fig. 2). In our method, the disparity distribution exhibits only a single prominent peak precisely at the ground truth disparity, whereas deconvolution may exhibit multiple peaks, potentially leading to incorrect disparity results.

²⁸⁵ *B. Implementation*

 Given an image pair, we extract multi-scale feature maps F_l at each level *l* for reference and target images. We then use the feature maps to construct the cost volume at the lowest level. As for the cost volume at the high level, we iteratively upsample the cost volume from the low level to the high level through two steps, the inter-scale similarity measurement, and the stereo-content-aware cost aggregation. The inter-scale similarity measurement uses feature maps from adjacent scales to generate similarity guidance. The stereo-content-aware cost aggregation uses the similarity guidance from two views to guide the cost volume upsampling. At last, we use the cost volume at the highest level to compute the disparity map as the output of our network. Fig. 3 illustrates the pipeline of our ²⁹⁹ method.

³⁰⁰ *1) Inter-Scale Similarity Measurement:* The inter-scale sim-301 ilarity measurement takes the feature maps F_l and F_{l-1} as input. We compute the similarity by the summation of the input. We compute the similarity by the summation of the

products of $F_l(h', w')$ and the neighbors of $F_{l-1}(h, w)$ with 303 the formula as 304

$$
S_l(h', w') = \frac{1}{M \cdot M} \phi\left(\sum_{(h, w) \in \mathcal{N}_F} F_l(h', w') F_{l-1}(h, w)\right), \quad (5) \quad \text{as}
$$

where (h', w') and (h, w) are the location at high-level and 306 low-level respectively, $(h', w') = (h \cdot s, w \cdot s)$, *s* is the scale 307 change in resolution from level $l - 1$ to level l , and \cdot is the 308 scalar multiplication operation. $S_l \in \mathbb{R}^{H^l \times W^l}$ is the similarity ³⁰⁹ guidance at level *l*, $S_l(h', w')$ is the value of the pixel at σ ³¹⁰ location (h', w') , $\mathcal{N}_F \in \mathbb{R}^{M \times M}$ is a 2D neighborhood of the 311 pixel at location (h, w) with the size of $M \times M$. $\phi(\cdot)$ is a ³¹² subnetwork composed of convolution layers, relu layers, and ³¹³ subnetwork composed of convolution layers, relu layers, and batch normalization layers. 314

2) Stereo-Content-Aware Cost Aggregation: 3D convolution 315 based methods [6], [7] usually perform window based cost 316 aggregation: 317

$$
\mathbf{C}_l(h', w', d') = \sum_{(h, w, d) \in \mathcal{N}_c} W_l(h', w', d') \mathbf{C}_{l-1}(h, w, d), \quad (6) \quad \text{as}
$$

where \mathcal{N}_c is a 3D neighborhood of the point at \mathfrak{so} (*h*′ /*s*, w′ /*s*, *d*′ $/$ *s*). 320

In our method, we replace the 3D weight W_l with the 321 2D similarity guidance S_l . For each level, we use the feature 322 maps of the stereo images, i.e., reference and target images, 323 to compute the content-aware similarity guidance S_l^R and S_l^T *l* ³²⁴ by inter-scale similarity measurement, respectively. Then we 325 perform the cost aggregation guided by $S_l^{\overline{R}}$ and S_l^T : 326

$$
C_{l}(h', w', d') = \sum_{(h, w, d) \in \mathcal{N}_c} S_{l}^{R}(h', w') S_{l}^{T}(h', w' - d')
$$

$$
C_{l-1}(h, w, d)
$$
. (7) 328

The memory and computational cost of 3D cost aggregation ₃₂₉ are unaffordable. Accordingly, we introduce a decomposition 330 strategy to reduce the computation cost. We split the upsam-
331 pling in full 3D spatial-disparity space into 1D disparity and 332 2D spatial upsampling by leveraging the property of cost vol- ³³³ ume on the disparity dimension. The property is that position 334 (h, w, d) in cost volume represents the (h, w) in the reference 335 image and $(h, w - d)$ in the target image. We warp S_l^T to S_l^R , 336 and then split the mapping of cost volume into 1D disparity 337 dimension and 2D spatial dimension. Specifically, we replace 338 Eq. (7) with a two-step decomposed cost aggregation. 339

In the first step, 1D disparity upsampling, the positions 340 $(h, w, d - \lfloor M/2 \rfloor), \ldots, (h, w, d), \ldots, (h, w, d + \lfloor M/2 \rfloor)$ in $\frac{341}{2}$ cost volume along disparity dimension correspond to (h, w) cost volume along disparity dimension correspond to (h, w) in the reference image and $(h, w - d + |M/2|), \ldots, (h, w - 343)$ *d*), ..., $(h, w - d - |M/2|)$ in the target image. Formally, the 344 updating along the disparity dimension is given by 345

$$
C_l(h, w, d') = \sum_{d \in \mathcal{N}_d} S_l^R(h', w') S_l^T(h', w' - d') C_{l-1}(h, w, d),
$$

$$
(8) \qquad 347
$$

where $\mathcal{N}_d = \{d'/s - \lfloor M/2 \rfloor, \ldots, d'/s, \ldots, d'/s + \lfloor M/2 \rfloor\}.$ 348 In the second step, 2D spatial upsampling, all voxels with ³⁴⁹ location $(h', w', :)$ in cost volume correspond to the pixel with $\frac{350}{250}$

Fig. 3. The overall architecture. Given an image pair, our method extracts multi-scale features at each level *l*. *L* is the total number of levels. \circledR is the warping operation used for generating the initial cost volume in the lowest resolution. \otimes represents element-wise multiplication.

 λ_{351} location (h', w') in the reference image. The update along the ³⁵² spatial dimension is given by

$$
C_l(h', w', d') = \sum_{(h,w)\in\mathcal{N}_{sp}} S_l^R(h', w') C_l(h, w, d'), \qquad (9)
$$

³⁵⁴ where $\mathcal{N}_{sp} \in \mathbb{R}^{\mathbb{M} \times \mathbb{M}}$ is a 2D neighborhood of the pixel with \log_5 location $(h'/s, w'/s)$ at level $l - 1$.

³⁵⁶ After all these operations, we complete the transformation f_{357} from the shape of $H_{l-1} \times W_{l-1} \times D_{l-1}$ to $H_{l-1} \times W_{l-1} \times D_l$ and then to $H_l \times W_l \times D_l$, where $H_l = H_{l-1} \cdot s$, $W_l = W_{l-1} \cdot s$ 359 and $D_l = D_{l-1} \cdot s$.

 3) Loss Function: We use a multi-scale loss function that applies smooth L_1 loss to each level. The smooth L_1 loss function is not sensitive to outliers or noises. The loss function is defined as

$$
D_l = \sum_{d \in (d+1)^N} d \cdot \sigma(-C_l), \qquad (10)
$$

$$
l - \sum_{d \in \{d_n\}_{n=1}^N}
$$

 $\mathcal{L} = \sum_{l=1}^{d \in \{a_n\}} \lambda_l$ *l*=0 $\mathcal{L} = \sum \lambda_l \cdot \mathcal{L}_l (\mathbf{D}_l - \mathbf{G}_l),$ (11)

$$
\mathcal{L}(\mathcal{L})
$$

$$
\mathcal{L}_l(x) = \begin{cases} 0.5 \ x^2, & \text{if } |x| < 1\\ |x| - 0.5, & \text{otherwise} \end{cases}
$$
 (12)

where $\{d_n^l\}_{n=1}^N$ is the disparity hypothesis at level *l*, $\sigma(\cdot)$ is the softmax operation, D_l is the predicted disparity map at level *l*, λ_l denotes the coefficients for the disparity prediction at level σ _{*l*}, and G_l is the ground-truth disparity map at level *l*.

³⁷¹ *C. Computational Cost Analysis*

372 To further demonstrate the superiority of our decomposition strategy in computational complexity, we conducted the fol- lowing analysis and complexity experiments (in Section V). We separate the 3D upsampling into 1D upsampling plus 2D upsampling, reducing the parameters and calculations.

1) Parameters: For deconvolution, the number of param- 377 eters per layer is given by $C \times 1 \times k^3 = Ck^3$, where *k* is 378 the kernel size, C is the number of input channels, and the 379 output channel is set to 1. In contrast, our method requires 380 $Ck²$ parameters per layer. Both our method and deconvolution $\frac{381}{2}$ utilize the same number of layers. 382

2) Calculations: For the computational complexity of 3D ³⁸³ upsampling, comparing 3D deconvolution with our method for 384 a feature volume of size $C \times D \times H \times W$ to be upsampled 385 by a scale of *s*, the computational cost for deconvolution 386 is $\mathcal{O}(s^3k^3)CDHW$, while ours is $\mathcal{O}(s^2k^2 + sk)CDHW = \infty$ $\mathcal{O}(s^2k^2)\mathcal{C}DHW$.

V. EXPERIMENTS 389

A. Datasets 390

1) SceneFlow Dataset: SceneFlow [29] is a large synthetic 39 dataset containing 34896 training images and 4248 testing 392 images with the size of 540×960 . This dataset has three 393 rendered sub-datasets: FlyingThings3D, Monkaa, and Driving. ³⁹⁴ FlyingThings3D is rendered from the ShapeNet dataset and ³⁹⁵ has 21828 training data and 4248 testing data. Monkaa is 396 rendered from the animated film Monkaa and has 8666 training 397 data. The Driving is constructed by the naturalistic, dynamic 398 street scene from the viewpoint of a driving car and has 399 4402 training samples. 400×400

2) KITTI 2015 Dataset: KITTI 2015 [61] is a real-world ⁴⁰¹ dataset with street views from a driving car. It contains ⁴⁰² 200 training stereo image pairs with sparse ground-truth dis- ⁴⁰³ parities obtained using LiDAR and another 200 testing image 404 pairs without ground-truth disparities. During the training pro- ⁴⁰⁵ cess, we take 160 images for training and reference 40 images ⁴⁰⁶ for validation. 407

3) Middlebury-v3 Dataset: Middlebury-v3 is a subset of the 408 2014 dataset [62] and is collected in the real world with static 409 indoor scenes containing complicated and rich details. There 410 are 15 stereo pairs for training and 15 stereo pairs for testing. ⁴¹¹ ⁴¹² Each pair is provided in 3 kinds of resolution, full, half, and ⁴¹³ quarter resolution; where we used the quarter resolution in the ⁴¹⁴ experiment.

 4) ETH3D-Two-Iew Dataset: ETH3D (two view) [63] com- prises grayscale stereo pairs captured from diverse indoor and outdoor scenes. The dataset includes 27 training and 20 testing image pairs with sparsely labeled ground truth. Disparities range from 0 to 64 pixels, and bad 1.0 (percentage of pixels with errors larger than 1 pixel) are reported.

⁴²¹ *B. Evaluation Metrics*

c prior grap state pairs are point and the state based of the state of the s The end-point error (EPE) is the mean disparity error in pixels. The 3-px error refers to the proportion of points in the full map where the absolute value of the differ- ence between the predicted disparity and the true value is greater than 3 pixels. The percentage of disparity outliers in the background (*D1-bg*), foreground (*D1-fg*), or all pixels (*D1-all*) for both noc regions and all regions are applied for evaluation. Disparity outliers are the pixels if their disparity EPE is more than 3 or 5% pixels. *avgerr* is the average absolute error in pixels. *RMS* represents the root mean square of the differences between the estimated and actual disparities. *A90* and *A95* are the 90% and 95% error quantile in pixels, respectively. *Bad 1.0* and *Bad 2.0* percentage of pixels with errors larger than 1 pixel or 2 pixels, respectively.

⁴³⁶ *C. Model Details*

 To prove the effectiveness of our method, we extend five stereo baseline networks with our method, CF-Net [30], HSM- Net [7] and PSM-Net [6], FastAcv [44] and FastAcvPlus [44]. All networks are implemented via PyTorch and tested on NVIDIA RTX 3090 GPU. For all baselines, the neighborhood size *M* is set to the scale change *s* at each level.

 For PSM-Net+ours, the model is optimized using Adam [64] with β_1 of 0.9, β_2 of 0.999. During training, the batch size is fixed to 8, and we perform color normalization to each input 446 image and crop them into 256×512 resolution. We train our network on SceneFlow for 10 epochs and change the learning rate from 0.001 to 0.0001 in the 7th epoch. We then fine- tune the network on KITTI 2015 and set the learning rate to 0.001, 0.0001, and 0.00003 in the first 200 epochs, the next 400 epochs, and the final 600 epochs, respectively. As for Middlebury-v3, we also fine-tune the model pre-trained on SceneFlow. The learning rate is set to 0.001 for 300 epochs and then changed to 0.0001 for the rest of 600 epochs. For HSM-455 Net+ours, we use AdamW [65] with β_1 of 0.9, β_2 of 0.999. During training, the batch size is fixed to 12, and we perform the same data augmentation [7] of the original HSM-Net and 458 crop the images into 256×512 resolution. We train our network for 10 epochs using the same dataset as HSM-Net and change the learning rate from 0.001 to 0.0001 in the 9th epoch. For CF-Net, FastAcv, and FastAcvPlus, we follow all the training strategies of the official repositories.

Furthermore, we downsample the ground truth for our multi-⁴⁶⁴ scale loss. We use bilinear downsampling in SceneFlow and ⁴⁶⁵ nearest downsampling in KITTI 2015 and Middlebury-v3.

TABLE I EVALUATION RESULTS OF CURRENT STEREO MATCHING ALGORITHMS ON THE SCENEFLOW TEST SET

Model	PSM-Net [6] (2018)	Gwc-Net [13] (2019)	HSM-Net [7] (2019)
EPE(px)	1.09	0.98	2.07
Model	Acf-Net (2020)	LEAStereo (2020)	CF-Net (2021)
EPE(px)	0.87	0.78	0.99
Model	$LaC+ GwcNet (2022)$	LaC+ GANet (2022)	FastAcv (2023)
EPE(px)	0.75	0.72	0.64
Model	FastAcvPlus (2023)	PSM-Net+ours	HSM-Net+ours
EPE(px)	0.59	0.63	1.39
Model	CF-Net+ours	$FastAcv + ours$	FastAcvPlus + ours
EPE(px)	0.72	0.59	0.57

Additionally, we reduced the computational cost without sacri-
466 ficing accuracy by moving the averaging operation before the 467 aggregation at each layer. Although we observe better results 468 of bilinear downsampling in the experiment on SceneFlow, the ⁴⁶⁹ ground truth disparities of the two real-world datasets contain 470 invalid values, like 0 and INF, which will lead to wrong disparity results after bilinear downsampling. In all experiments, 472 no post-processing or unsupervised learning methods are used. 473

D. Comparison With Stereo Matching Methods ⁴⁷⁴

Our method mainly focuses on recovering the fine-grained 475 details lost during cost volume downsampling. Therefore, ⁴⁷⁶ we conduct experiments on the SceneFlow dataset, specifi-477 cally targeting fine-grained areas, and we compare the results 478 against mainstream baseline methods. Additionally, we per- ⁴⁷⁹ form experiments on real datasets, including KITTI and ⁴⁸⁰ Middlebury, to validate the effectiveness of our approach. 481

1) SceneFlow: The experimental results in Table I ⁴⁸² show that our proposed method significantly improves 483 the performance of stereo matching algorithms, with the ⁴⁸⁴ FastAcvPlus+ours achieving the lowest EPE of 0.57. The consistent reduction in EPE across various models demonstrates 486 the robustness and efficacy of our method. 487

a) Fine-grained areas: We test different baselines in the 488 fine-grained region on the SceneFlow dataset to verify the 489 accuracy improvement of our method in the fine-grained (FG) ⁴⁹⁰ areas and full areas, as shown in Table II. We use the calculated $_{49}$ HOG [66] descriptor of the reference image as a mask of fine- ⁴⁹² grained areas. The results in Table II show the superiority of 493 our method in fine-grained areas. Our method can improve ⁴⁹⁴ the accuracy significantly in fine-grained areas, and 37.6%, ⁴⁹⁵ 32.9%, 16.2%, 11.4% and 10.4% EPE reduction in PSM-Net, ⁴⁹⁶ HSM-Net, CF-Net, FastAcv and FastAcvPlus, respectively. ⁴⁹⁷ Our method is effective for different baselines with good ⁴⁹⁸ universality. Our method also brings no or small increase in ⁴⁹⁹ runtime. For PSM-Net, we remove the time-consuming 3D 500 convolution layers in the hourglass modules at RES 1/16 and 501 RES 1/8. For the rest baselines, we directly plug our method 502 into them without additional model modification. 503

The visualization results for the fine-grained regions are 504 depicted in Fig. 4. Our method successfully recovers more 505 details, notably improving estimation results for fine-grained 506 areas like the spokes of the wheel and plant spikes in the 507 left column of Fig. 4 compared to the baseline. Furthermore, $\frac{508}{200}$ our approach enhances results in less refined regions, such as $_{509}$ inside the bounding box in the right column of Fig. 4. $\frac{510}{200}$

TABLE II

RESULTS OF DIFFERENT BASELINE IN FULL AREAS (FULL) AND FINE-GRAINED (FG) AREAS ON THE SCENEFLOW DATASET. FOR PSM-NET, WE REMOVE THE TIME-CONSUMING 3D CNNS AT RES 1/16 AND RES 1/8

Method	EPE in Full	EPE in FG	Time (s)
PSM-Net [6] (2018)	1.09	1.01	0.41
PSM-Net+ours	0.60	0.63	0.37
HSM-Net [7] (2019)	1.88	2.07	0.05
HSM-Net+ours	1.25	1.39	0.09
CF-Net [30] (2021)	1.06	0.99	0.18
CF-Net+ours	0.72	0.83	0.22
FastAcv [44] (2023)	0.64	0.70	0.05
FastAcv+ours	0.59	0.62	0.08
FastAcvPlus [44] (2023)	0.59	0.67	0.05
FastAcyPlus+ours	0.57	0.60	0.08

Fig. 4. The results of PSM-Net [6] and PSM-Net+ours on the SceneFlow dataset.

 b) Full areas: Our method brings improvement for full areas across different baselines. Visualization of the results (Fig. 5) reveals that our method exhibits certain corrective effects on large-scale weakly-textured regions as well. The experimental results demonstrate that our approach achieves significant accuracy improvement when applied to datasets with complete depth information as ground truth.

 2) Kitti: Table III displays the performance and runtime of various algorithms evaluated on the KITTI stereo2015 benchmark. Across different baselines, our method enhances the accuracy of the original baselines with only a marginal increase in processing time. Notably, CF-Net combined with our method surpasses other competing methods in the Noc D1-all and All D1-all. Next, we would like to provide a more detailed explanation of the comparison between our method and stereo matching methods based on attention mechanisms, as well as methods based on decomposition strategies.

TABLE III

EVALUATION ON KITTI 2015 BENCHMARK. THE BEST RESULTS FOR EACH EVALUATION METRIC ARE SHOWN IN BOLD

		Noc $(\%)$		All $(\%)$			
Models	bg	fg	all	bg	fg	all	Time (s)
PSM-Net [6] (2018)	1.71	4.31	2.14	1.86	4.62	2.32	0.41
GwcNet-g [13] (2019)	1.61	3.49	1.92	1.74	3.93	2.11	0.32
HSM-Net [7] (2019)	1.63	3.40	1.92	1.80	3.85	2.14	0.05
RAFT-Stereo [8] (2021)	-	٠	$\overline{}$	2.89	1.75	1.96	
HDA-Net [67] (2021)	1.55	3.32	1.84	1.69	3.76	2.03	0.42
BG-Net [48] (2021)	1.91	4.34	2.31	2.07	4.74	2.51	0.02
Dec-Net [31] (2021)	1.89	3.53	2.16	2.07	3.87	2.37	0.05
CF-Net [30] (2021)	1.43	3.25	1.73	1.54	3.56	1.88	0.18
ChiT-12 [42] (2022)	2.11	3.79	2.38	2.34	4.05	2.60	
FC-PSMNet [39](2022)	1.73	4.19	2.13	1.86	4.61	2.32	
HTSGM [49] (2022)			5.66			5.84	
FastACV-Plus [44] (2023)	۰	$\overline{}$	۰	1.70	3.53	2.01	0.05
PSM-Net+ours	1.50	3.42	1.82	1.73	3.78	2.07	0.38
HSM-Net+ours	1.64	3.21	1.90	1.77	3.60	2.09	0.10
CF-Net+ours	1.46	2.95	1.70	1.58	3.30	1.87	0.22

a) Compared with the attention-based method: HDA- ⁵²⁸ Net [67] proposes an efficient horizontal attention module 529 to adaptively capture the global correspondence clues. Our 530 method uses inter-scale information to generate similarity 531 guidance to improve cost aggregation. As shown in Table III, 532 our method has lower D1-all (HDA-Net 2.03 *vs.* CF-Net+Ours 533
1.87) with faster running time (HDA-Net 0.42ms *vs.* 534 1.87) with faster running time (HDA-Net 0.42ms *vs.* $CF-Net+Ours$ 0.22ms) on the KITTI 2015 dataset.

b) Compared with the decomposition method: DecNet 536 [31] decomposes the original stereo matching into a dense 537 matching at the lowest resolution and a series of sparse 538 matching at higher resolutions. Unlike DecNet, our method 539 decomposes the 3D upsampling of cost volume into a 2D- ⁵⁴⁰ spatial and 1D-disparity upsampling. Our method outperforms 541 DecNet in D1-all (Dec-Net 2.37 *vs.* HSM-Net+Ours 2.09) 542 but is slower in runtime (Dec-Net 0.05ms *vs.* HSM-Net+Ours 543 0.09 ms), as shown in Table III. 544

c) Visualization: Fig. 6 presents the experimental results 545 on the KITTI 2015 dataset, showcasing images from top to ⁵⁴⁶ bottom. Our method excels in recovering slender structures, 547 as seen in the iron chain at the center of the first row and ⁵⁴⁸ the fence in the lower left corner of the third row. Moreover, ⁵⁴⁹ our approach accurately estimates depth-mutation areas such 550 as signboards and utility poles. For instance, unlike PSM-Net 551 and HSM-Net in the first row's bounding box around the 552 signboard, our method produces correct results. In rows two, 553 five, and six, the other methods misidentify parts of the 554 background as utility poles, which our method avoids. 555

3) Middlebury: We compare our method with several 556 approaches using different aggregation strategies on the Mid- 557 dlebury stereo dataset v3, as shown in Table IV. We outperform 558 these 3D aggregation based approaches on most of the met- ⁵⁵⁹ rics. The result also demonstrates the effectiveness of our ⁵⁶⁰ content-aware upsampling method. Based on the visualizations 561 in Fig. 7, we can draw the following conclusions: 1) **Improved** $_{562}$ depth estimation for fine-grained regions: Our method ⁵⁶³ shows superior performance in depth estimation for fine- ⁵⁶⁴ grained regions, demonstrating the effectiveness of explicitly 565 integrating high-resolution and low-resolution information. ⁵⁶⁶ This is evident in almost all cases, such as the detailed areas 567

Fig. 5. The visualization of results on HSM-Net baseline. The first and second columns are the reference input images and ground truth. The rest columns are results from HSM-Net and HSM-Net+ours.

Fig. 6. The results of different deep stereo networks on KITTI 2015 dataset. Our method performs better in fine-grained areas than other methods, especially for the region denoted with the boxes. Please zoom in to check the details.

 in "DjembL" and the water cup on the table in "Crusade" (Line 3, PSM-Net vs. PSM-Net + ours), as well as the small figurine (Line 3, HSM-Net vs. HSM-Net + ours).
 571 2) Enhanced foreground and background decoupling: Our 2) Enhanced foreground and background decoupling: Our method has a stronger ability to decouple the foreground from the background. Retaining low-resolution information effec- tively enhances this capability. Examples include the depth estimation of the potted plants and background in "Plants" (Line 5) and the estimation of the hollow part of the staircase handrail in "Staircase" (Line 4, HSM-Net vs. HSM-Net + ours; CF-Net vs. CF-Net + ours). 3) Competitive perfor- mance in flat regions: Our method also shows competitive performance in flat regions. For instance, the wall in the upper left of "Staircase" (Line 4, PSM-Net vs. PSM-Net + ours)

and the restoration of the table corner in "Crusade" (Line 3, ⁵⁸² $CF-Net$ vs. $CF-Net + ours$). However, our method has some 583 shortcomings in certain areas, such as the seats in the PSM-Net 584 case of "Classroom2E" (Line 1, PSM-Net vs. PSM-Net $+$ 585 ours). We will systematically discuss these limitations in the 586 Limitation Analysis section. 587

E. Ablation Studies 588

We conduct all the analysis in ablation studies mainly on 589 the HSM-Net baseline. Ablation studies are performed on the 590 SceneFlow dataset and the KITTI 2015 dataset. 591

1) Effectiveness of Stereo-Content-Aware Cost Aggregation: ⁵⁹² During Stereo-Content-Aware Cost Aggregation, we use both 593

Fig. 7. The visualization of results on Middlebury-v3 test set. In the first column are the reference input images. The rest columns are results from PSM-Net [6], PSM-Net + ours, HSM-Net [7], + ours, CF-Net [30] and CF-Net + ours respectively.

TABLE IV EVALUATION ON MIDDLEBURY-V3. THE BEST RESULTS FOR EACH EVALUATION METRIC ARE SHOWN IN BOLD

Models	Res	Avgerr	Rms	A90	A95
PSM-Net ROB (2018) [6]	О	8.78	23.3	22.8	43.4
DeepPruner (2019) [68]	О	6.56	18	17.9	33.1
FADNet++ (2021) [69]	O	11.9	27.7	34.3	61.2
MCP-HA-VO (2022) [70]	O	6.01	37.5	40.6	85.9
H-CENST (2022) [71]	O	10.2	29.1	24.3	59.0
FM-DT (2023) [72]	O	11.7	31.4	33.4	67.1
PSM-Net+ours		5.43	17.3	8.11	25.2

 reference and target images to extract similarity guidance and separate the 3D spatial-disparity upsampling into 1D dispar- ity / 2D spatial upsampling. We evaluate the effectiveness of our method at different resolutions through two experiments: i. Training on the SceneFlow dataset and testing on the SceneFlow dataset. ii. Training on the SceneFlow dataset and testing on the validation set of the KITTI 2015 dataset. Table V demonstrates that our decomposition strategy reduces the running time by nearly half compared to full 3D upsampling at the setting of "RES 1/16 to RES 1/8" and "RES 1/8 to RES 1" on the SceneFlow dataset and KITTI 2015 dataset. Our decomposition strategy not only proves to be faster but also more accurate than full 3D upsampling. When integrating our method at "RES 1/16 to 1/8," HSM-Net+ours experiences a decrease in EPE of 18.09% and 15.86% compared to the original HSM-Net on the SceneFlow dataset and the KITTI 2015 dataset, respectively. Plugging our method at higher resolutions, i.e., "RES 1/8 to 1", the EPE of HSM-Net+ours is 33.51% and 26.21% lower than the original HSM-Net on the SceneFlow dataset and the KITTI 2015 dataset, respectively. Our method is effective and the higher the resolution at which 615 we employ our method, the greater the improvement it brings.

2) Effectiveness of Inter-Scale Similarity Measurement: ⁶¹⁶ We utilize inter-scale similarity measurement to generate a_{617} similarity guidance map for cost aggregation. Each pixel in the 618 similarity map corresponds to the content information at the 619 same location. Our method calculates the similarity between 620 high-resolution feature points and their corresponding $M \times M$ 621 points in the low-resolution counterpart. Visualizations of 622 similarity maps of a 3 size neighborhood are shown in Fig. 8. ϵ_{23}

We confirm the effectiveness of our inter-scale policy on 624 the SceneFlow dataset through a series of experiments. These 625 experiments are conducted in three settings: without sim- ⁶²⁶ ilarity guidance, with single-scale similarity guidance, and 627 with inter-scale similarity guidance. The results presented 628 in Table VI clearly demonstrate that the use of inter-scale 629 similarity guidance results in higher accuracy when com- 630 pared to single-scale similarity guidance. The inter-scale 631 similarity guidance transforms the unary mapping inherent 632 in single-scale similarity guidance into a pair-wise map- ⁶³³ ping, consequently leading to improved accuracy. Furthermore, ⁶³⁴ we verify the significance of employing stereo information, 635 which includes both reference and target images, to achieve 636 favorable results. In Table VI, it is evident that the EPE when 637 using stereo information is significantly lower than when not 638 using stereo information. Utilizing stereo information to model 639 the mapping relationship between cost volumes of different 640 resolutions proves to be more reliable than relying solely on 64 reference images. 642

3) Effectiveness of Our Method in Different Resolution: ⁶⁴³ We further provide visualizations of the results obtained from 644 HSM-Net and HSM-Net+ours at different resolutions on the 645 SceneFlow dataset. These visualizations help us understand 646 how our model enhances the baseline at various resolutions, 647 as shown in Fig. 9. At a resolution of 1/32, HSM-Net ⁶⁴⁸

TABLE V

RESULTS OF USING THE GUIDANCE IN MULTIPLE STEPS OF MULTI-SCALE COST AGGREGATION ON SYNTHETIC AND REAL DATASETS. RES 1/16, 1/8, 1 REPRESENTS THE ORIGINAL IMAGE'S 1/16, 1/8, AND 1 RESOLUTION. RES 1/16 TO 1/8 INDICATES WHETHER THE BASELINE IS PLUGGED WITH OUR METHOD IN COST AGGREGATION FROM RESOLUTION 1/16 TO RESOLUTION 1/8, SO AS RES 1/8 TO 1

Models	Inter-scale		3D upsampling		SceneFlow		KITTI 15	
	RES $1/16$ to $1/8$	RES $1/8$ to 1	Full 3D	$2D + 1D$	EPE	Times (s)	EPE	Times (s)
HSM				$\overline{}$	l.88	0.05	1.45	0.05
HSM+ours		-		$\overline{}$	1.81	0.17	1.37	0.18
HSM+ours		-			.54	0.06	1.22	0.08
HSM+ours				\sim	67	0.27	1.32	0.24
HSM+ours			\sim		.25	0.09	1.07	0.10

Fig. 8. The visualization of similarity. (a) and (b) are the similarity of the two images. The three columns on the right are visualizations of the similarity, representing the similarity of points in high resolution to their corresponding neighbors in low-resolution projection points. In each map, the brightness indicates the similarity, which corresponds to the upsampling kernel weight. It can be seen that the aggregation weight is directly related to the image content and that each weight in the global picture uniquely adapts the content information of the corresponding points.

TABLE VI

THE RESULTS OF USING DIFFERENT SCALES OF GUIDANCE TO GUIDE COST AGGREGATION. "INTER-SCALE" AND "SINGLE-SCALE" REP-RESENT THAT THE GUIDANCE MAPS ARE GENERATED FROM ADJACENT SCALES OR A SINGLE SCALE, RESPECTIVELY. THE "STEREO INFO" INDICATES WHETHER THE GUIDANCE MAPS ARE GENERATED WITH STEREO INFORMATION INCLUDING BOTH REFERENCE AND TARGET IMAGE FEATURES, OR ONLY FEATURES OF THE REFERENCE IMAGES

 exhibits a failure in recovering the objects within the white bounding box, but our method successfully rectifies this error. Additionally, our method corrects the gaps within the blue bounding box at a resolution of 1/16. From a resolution of 1/32 to 1, our method effectively recovers the triangular area within the black bounding box. It is evident that high-resolution cost aggregation is markedly influenced by low-resolution cost aggregation. Our method systematically addresses errors in the original method at each resolution, commencing with the lowest resolution.

⁶⁵⁹ *F. Generalization Evaluation*

⁶⁶⁰ *1) Universality of Cost Aggregation Method on Different* ⁶⁶¹ *Baseline:* We apply our method to five stereo networks, i.e.,

PSM-Net [6], HSM-Net [7], and CF-Net [30], FastAcv [44] 662 and FastAcvPlus [44] to verify the university of our method. 663 The results on the SceneFlow dataset are shown in Table II, 664 and the results on the KITTI 2015 dataset are shown in 665 Table III. 666

For PSM-Net, HSM-Net, and CF-Net, our methods have 667 improved by 44.5% , 33.5% , and 32.1% on the SceneFlow 668 dataset, respectively. Moreover, our method has achieved 669 reductions in D-all metrics for all three baselines on the 670 KITTI 2015 dataset. Our method consistently enhances various 671 baselines on both synthetic and real datasets. 672

2) Zero-Shot Generalization Ability: Obtaining large-scale 673 real-world datasets for training is challenging, making the ⁶⁷⁴ generalization capability of stereo models crucial. To this end, 675 we evaluate the generalization performance of our methods 676 from synthetic datasets to unseen real-world scenes. In this 677 evaluation, we train various baseline models augmented with 678 our approach on the Scene Flow dataset and directly evaluate 679 them on the Middlebury 2014 and ETH3D training sets. 680 As shown in Table VII, our method consistently outper- 681 forms all baselines, demonstrating its strong generalization 682 capability.

G. Comparison With Content-Aware Upsamping Methods ⁶⁸⁴

To demonstrate our superiority over conventional ⁶⁸⁵ content-aware upsampling operators, we directly applied 686 $CARAFF++$ [59] to the HSM-Net baseline for comparative $\frac{687}{687}$
analysis. The content-aware operators were implemented $\frac{687}{688}$ analysis. The content-aware operators were implemented at resolutions of $\frac{1}{32}$, $\frac{1}{16}$, and $\frac{1}{8}$ of full resolution, aligning 689

Fig. 9. Results of HSM-Net and HSM-Net+ours at different resolutions. We obtain the disparity map by regressing the cost volume at each resolution.

 with the settings of our method. We conducted training and testing of HSM-Net with CARAFE++ on the SceneFlow dataset, using EPE as the measurement metric. The results presented in Table VIII clearly indicate that our method outperforms CARAFE++ in terms of accuracy and speed. Inter-scale information provides us with a broader receptive field for aggregation and access to more content information. Furthermore, our approach involves separating the 3D upsampling process into 1D and 2D upsampling, resulting in a significant reduction in computational ⁷⁰⁰ cost.

1) Complexity Analysis: To further demonstrate the supe- 701 riority of our decomposition strategy in computational ⁷⁰² complexity, we conducted the following analysis and com- ⁷⁰³ plexity experiments. We separate the 3D upsampling into ⁷⁰⁴ 1D upsampling plus 2D upsampling, reducing the parameters 705 and calculations. We test the memory cost of different cost 706 aggregation methods of HSM-Net in $\frac{1}{8}$ and 1 of the full $\frac{707}{207}$ resolution (540 \times 960) of the SceneFlow dataset and the results τ ₀₈ are shown in Table IX. At the same resolution, our module 709 exhibits lower memory and time consumption compared to $\frac{710}{20}$ the other two upsampling methods. $\frac{711}{200}$

TABLE VII TABLE IX SYNTHETIC TO REAL GENERALIZATION EXPERIMENTS. ALL MODELS ARE TRAINED ON SCENE FLOW. THE BAD 2.0 ERROR RATE IS USED FOR MIDDLEBURY-V3, AND THE BAD 1.0 ERROR RATE FOR ETH3D

		Middlebury		(a) CF Net + ours
Model	H-res	Q-res	ETH3D	
PSM-Net $[6]$ (2018)	15.8	9.8	10.2	
GA-Net [45](2019)	13.5	8.5	6.5	Sparse ground-truth No ground-truth area
HSM-Net [7] (2019)	11.9	7.9	6.7	
DSM-Net [73] (2020)	13.8	8.1	6.2	
CF-Net [30] (2021)	15.3	9.8	5.8	
FC-GANet [39](2022)	10.2	7.8	5.8	
FastAcv [44](2023)	12.0	10.6	11.8	
FastAcvPlus [44] (2023)	12.4	10.2	11.8	(b) Ground-truth in KITTI 2015 dataset (training split)
$PSM-Net + ours$	13.5	7.8	7.1	
$HSM-Net + ours$	9.8	6.2	5.6	Fig. 10. Failure case and ground-truth in the outdoor scenarios.
$CF-Net + ours$	12.3	7.2	4.6	
FastAcv + ours	11.0	10.1	10.2	
FastAcvPlus + ours	10.7	8.9	9.9	within extensive textureless areas, which will sign
				bolster the performance in outdoor environments. Furt
				the present study has adopted a distinct spatial doma
	TABLE VIII			eling strategy to address the issue of detail loss.
RESULT OF COMPARISON BETWEEN CARAFE++ [59] AND OURS IN				utilization of high-frequency components in the fi
BASELINE HSM-NET [7]. BOTH CARAFE++ AND OURS ONLY REPLACE THE UPSAMPLING MODULE AT RES 1/16 TO 1/8				domain for such fine-grained information presents
				an inherently viable alternative. Moving forward, w
Experiments Raw [7] Baseline \checkmark	CARAFE++ [59]	EPE Ours 1.88	Time(s) 0.05	
Baseline	✓	1.81	0.15	to experiment with frequency domain analysis ted
Baseline		1.54 \checkmark	0.06	including wavelet transformations, to facilitate the re
				of fine-grained regional information.
	TABLE IX			
(COMPLEXITY AND EFFICIENCY ANALYSIS OF DIFFERENT COST AGGRE-				VI. CONCLUSION
GATION STRATEGIES (THE BASELINE MODEL IS HSM-NET). DUE TO				
HARDWARE LIMITATIONS, WE DO NOT RUN CARAFE++ AT 1/8				We have presented an inter-scale similarity guid
TO 1 RESOLUTION. THE BEST RESULTS FOR EACH EVALUATION				aggregation method designed to adaptively recove
METRIC ARE SHOWN IN BOLD				in fine-grained areas. By leveraging both low-ro
Resolution (RES) Upsampling			Memory (MB) Extra Parameter (KB) Times (s)	and high-resolution information, our approach ef
$rac{1}{16}$ to $rac{1}{8}$ $rac{1}{8}$ to 1 $HSM + CARAFE++[52]$	5153.81	467	0.15	exploits detail while generating inter-scale similarity
$HSM + 3D$ Deconv	1574.71	216	0.08	ments. Additionally, our stereo-content-aware cost agg
$HSM + Ours$ $HSM + CARAFE++[52]$	1094.86	113	0.06	method employs a decomposition strategy that divide
$HSM + 3D$ Deconv √	10936.72	216	0.20	
HSM + Ours	7988.72	113	0.09	disparity-spatial space into 1D disparity space and 2l
				space, significantly reducing computational costs as
				with 3D cost volumes. Experimental results acro
H. Limitation				benchmarks demonstrate the effectiveness of our met
1) Lack of Dense Outdoor Data: The performance gains				various models.
for outdoor scenes are smaller compared to those in virtual				
and indoor datasets. Additionally, in the CF-Net baseline, our				REFERENCES
method still fails to completely correct the erroneous depth				[1] R. Chabra, J. Straub, C. Sweeney, R. Newcombe, and
estimation for the sky, as shown in Fig. 10 (a). We believe there				"StereoDRNet: Dilated residual StereoNet," in Proc. IEEE/

TABLE VIII

TABLE IX

⁷¹² *H. Limitation*

 1) Lack of Dense Outdoor Data: The performance gains for outdoor scenes are smaller compared to those in virtual and indoor datasets. Additionally, in the CF-Net baseline, our method still fails to completely correct the erroneous depth estimation for the sky, as shown in Fig. 10 (a). We believe there are two main reasons for this: 1) Poor ground truth quality. Outdoor datasets like KITTI use LiDAR scanning, resulting in sparse depth maps. Ground truth is missing in areas beyond the LiDAR scan range, as shown in Fig. 10 (b). This sparsity affects model training. 2) Lack of fine-grained regions. Our method focuses on fine-grained areas, but the coarse nature of LiDAR scans in outdoor datasets means many details are overlooked. For this scenario, we believe that employing some advanced depth completion methods to refine sparse areas in the ground truth could be a reasonable approach.

⁷²⁸ *2) Future Work:* In future work, we aim to delve into ⁷²⁹ super-resolution techniques to augment the detail information

within extensive textureless areas, which will significantly 730 bolster the performance in outdoor environments. Furthermore, $\frac{731}{2}$ the present study has adopted a distinct spatial domain mod- ⁷³² eling strategy to address the issue of detail loss. Yet, the 733 utilization of high-frequency components in the frequency ⁷³⁴ domain for such fine-grained information presents itself as 735 an inherently viable alternative. Moving forward, we intend 736 to experiment with frequency domain analysis techniques, 737 including wavelet transformations, to facilitate the restoration 738 of fine-grained regional information.

VI. CONCLUSION 740

We have presented an inter-scale similarity guided cost $_{741}$ aggregation method designed to adaptively recover details 742 in fine-grained areas. By leveraging both low-resolution ⁷⁴³ and high-resolution information, our approach effectively $_{744}$ exploits detail while generating inter-scale similarity measure- ⁷⁴⁵ ments. Additionally, our stereo-content-aware cost aggregation $_{746}$ method employs a decomposition strategy that divides the 3D $\frac{747}{640}$ disparity-spatial space into 1D disparity space and 2D spatial ⁷⁴⁸ space, significantly reducing computational costs associated 749 with 3D cost volumes. Experimental results across three 750 benchmarks demonstrate the effectiveness of our method with 751 various models. 752

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